Program Optimization

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These Slides

- Overview
- Generally Useful Optimizations
 - Code motion/precomputation
 - Strength reduction
 - Sharing of common subexpressions
 - Removing unnecessary procedure calls
- Optimization Blockers
 - Procedure calls
 - Memory aliasing
- Optimizing In Larger Programs: Profiling
- Exploiting Instruction-Level Parallelism
- Dealing with Conditionals

Performance Realities

- There's more to performance than asymptotic complexity
- Constant factors matter too!
 - Easily see 10:1 performance range depending on how code is written
 - Must optimize at multiple levels:
 - algorithm, data representations, procedures, and loops
- Must understand system to optimize performance
 - How programs are compiled and executed
 - How to measure program performance and identify bottlenecks
 - How to improve performance without destroying code modularity and generality

Optimizing Compilers

- Provide efficient mapping of program to machine
 - register allocation
 - code selection and ordering (scheduling)
 - dead code elimination
 - eliminating minor inefficiencies
- Don't (usually) improve asymptotic efficiency
 - up to programmer to select best overall algorithm
 - big-O savings are (often) more important than constant factors
 - but constant factors also matter
- Have difficulty overcoming "optimization blockers"
 - potential memory aliasing
 - potential procedure side-effects

Limitations of Optimizing Compilers

- Operate under fundamental constraint
 - Must not cause any change in program behavior
 - Often prevents it from making optimizations when would only affect behavior under pathological conditions.
- Behavior that may be obvious to the programmer can be obfuscated by languages and coding styles
 - e.g., Data ranges may be more limited than variable types suggest
- Most analysis is performed only within procedures
- Whole-program analysis is too expensive in most cases
- Most analysis is based only on static information

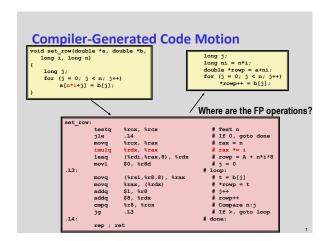
 Compiler has difficulty anticipating run-time inputs
- When in doubt, the compiler must be conservative

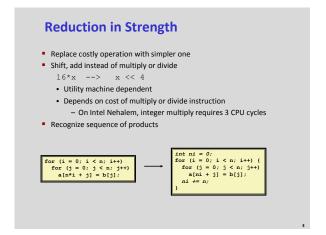
Generally Useful Optimizations

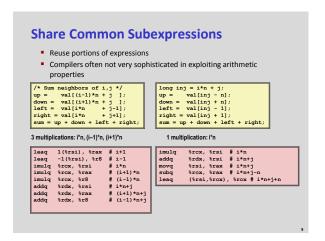
- Optimizations that you or the compiler should do regardless of processor / compiler
- (Loop Invariant) Code Motion
 - Reduce frequency with which computation performed
 - If it will always produce same result
 - Especially moving code out of loop

```
void set_row(double *a, double *b,
    long i, long n)
{
    long j;
    for (j = 0; j < n; j++)
        a[n*i+j] = b[j];
}
</pre>

    long j;
    int ni = n*i;
    for (j = 0; j < n; j++)
        a[ni+j] = b[j];
</pre>
```







```
Optimization Blocker #1: Procedure Calls

Procedure to Convert String to Lower Case

\[
\begin{align*}
\text{void lower(char *s)} \\
\text{int i;} \\
\text{for (i = 0; i < strlen(s); i++)} \\
\text{if (s[i] >= 'A' & & s[i] <= 'Z')} \\
\text{s[i] -= ('A' - 'a');} \end{align*}

Extracted from 213 lab submissions, Fall, 1998
```

```
    Time quadruples when double string length
    Quadratic performance

- Quadratic performanc
```

```
convert Loop To Goto Form

void lower(char *s)
{
    int i = 0;
    if (i >= strlen(s))
        goto done;
    loop:
        if (s[i] >= 'A' && s[i] <= 'Z')
            s[i] -= ('A' - 'a');
        i++;
        if (i < strlen(s))
            goto loop;
        done:
    }

strlen executed every iteration</pre>
```

Calling Strlen

```
/* My version of strlen */
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
        s++;
        length++;
    }
    return length;
}
```

- Strlen performance
 - Only way to determine length of string is to scan its entire length, looking for null character.
- Overall performance, string of length N
 - N calls to strlen
 - Require times N, N-1, N-2, ..., 1
 - Overall O(N²) performance

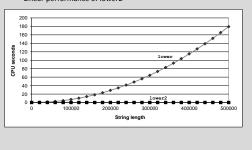
Improving Performance

```
void lower(char *s)
{
   int i;
   int len = strlen(s);
   for (i = 0; i < len; i++)
      if (s[i] >= 'A' && s[i] <= 'Z')
      s[i] -= ('A' - 'a');
}</pre>
```

- Move call to strlen outside of loop
- Since result does not change from one iteration to another
- Form of code motion

Lower Case Conversion Performance

- Time doubles when double string length
- Linear performance of lower2



Optimization Blocker: Procedure Calls

- Why couldn't compiler move strlen out of inner loop?
 - Procedure may have side effects
 - Alters global state each time called
 - Function may not return same value for given arguments
 - Depends on other parts of global state
 - Procedure lower could interact with strlen
- **■** Warning:
 - Compiler treats procedure call as a black box
 - Weak optimizations near them
- Remedies:
 - Use of inline functions
 - GCC does this with -O2
 - See web aside ASM:OPT
 - Do your own code motion

```
int lencnt = 0;
size_t strlen(const char *s)
{
    size_t length = 0;
    while (*s != '\0') {
        s++; length++;
    }
    lencnt += length;
    return length;
}
```

Exercise Break: Weird Pointers

■ Can the following function ever return 12, and if so how?

```
int f(int *p1, int *p2, int *p3) {
   *p1 = 100;
   *p2 = 10;
   *p3 = 1;
   return *p1 + *p2 + *p3;
}
```

Yes, for instance:

```
int a, b;
f(&a, &b, &a);
```

Memory Matters

```
/* Sum rows is of n X n matrix a
and store in vector b */
void sum rows1(double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        b[i] = 0;
        for (j = 0; j < n; j++)
            b[i] += a[i*n + j];
    }
}
```

```
# sum_rowsl inner loop
.L53:
addsd (%rcx), %xmm0  # FFP add
addq $8, %rcx
decq %rax
movad %xmm0, (%rei,%r8,8) # FFP store
jne .L53
```

- Code updates b [i] on every iteration
- Why couldn't compiler optimize this away?

Memory Aliasing

```
/* Sum rows is of n X n matrix a and store in vector b */ void sum rows! (double *a, double *b, long n) { long i, j; for (i = 0; i < n; i++) { b[i] = 0; for (j = 0; j < n; j++) b[i] += a[i*n + 3];
```

double A[9] = { 0, 1, 2, 4, 8, 16}, 32, 64, 128}; double B[3] = A+3; um rows1(A, B, 3)

```
i = 1: [3, 22, 16]
i = 2: [3, 22, 224]
```

Value of B:

init: [4, 8, 16]

- Code updates b [i] on every iteration
- Must consider possibility that these updates will affect program behavior

Removing Aliasing

```
/* Sum rows is of n X n matrix a
and store in vector b */
void sum rows2 (double *a, double *b, long n) {
    long i, j;
    for (i = 0; i < n; i++) {
        double val = 0;
        for (j = 0; j < n; j++)
        val += a[i*n + j];
        b[i] = val;
```

```
# sum_rows2 inner loop
.L66:
                        %rax
.L66
```

No need to store intermediate results

Optimization Blocker: Memory Aliasing

- Aliasing
 - Two different memory references specify single location
 - Easy to have happen in C
 - Since allowed to do address arithmetic
 - Direct access to storage structures
 - Get in habit of introducing local variables
 - · Accumulating within loops
 - Your way of telling compiler not to check for aliasing

What About Larger Programs?

- If your program has just one loop, it's obvious where to change to make it go faster
- In more complex programs, what to optimize is a key auestion
- When you first write a non-trivial program, it often has a single major algorithm performance problem
 - Textbook's example: insertion sort
 - Last program I wrote: missed opportunity for dynamic programming
 - Fixing this problem is way more important than any other changes

Amdahl's Law

- If you speed up one part of a system, the total benefit is limited by how much time that part took to start with
- Speedup S is:

$$S = \frac{1}{(1 - \alpha) + \alpha/k}$$

where the acceleration factor is k and the original time

Limiting case: even if k is effectively infinite, the upper limit on speedup is

$$S_{\infty} = \frac{1}{(1-\alpha)}$$

Knowing What's Slow: Profiling

- Profiling makes a version of a program that records how long it spends on different tasks
 - Use to find bottlenecks, at least in typical operation
- Common Linux tools:
 - gprof: GCC flag plus a tool to interpret output of the profiled program
 - Counts functions and randomly samples for time
 - Discussed in textbook's 5.14.1
 - Valgrind callgrind/cachegrind
 - Counts everything, precise but slow
 - OProfile
 - Uses hardware performance counters, can be whole-system

Exploiting Instruction-Level Parallelism

- Need general understanding of modern processor design
 - Hardware can execute multiple instructions in parallel
- Performance limited by data dependencies
- Simple transformations can have dramatic performance improvement
 - Compilers often cannot make these transformations
 - Lack of associativity and distributivity in floating-point arithmetic

```
Benchmark Example: Data Type for
Vectors
/* data structure for vectors */
typedef struct{
                                          len
                                                           0 1 len-1
     int len:
                                         data
 } vec;
 /* retrieve vector element and store at val */
int get_vec_element(*vec, idx, double *val)
      if (idx < 0 || idx >= v->len)
      return 0;

*val = v->data[idx];

return 1;
```

Benchmark Computation

```
void combine1(vec_ptr v, data_t *dest)
     *dest = IDENT;
     for (i = 0; i < vec length(v); i++) {
        data_t val;
       get_vec_element(v, i, &val);
*dest = *dest OP val;
```

Compute sum or product of vector elements

■Data Types

Use different declarations for data_t

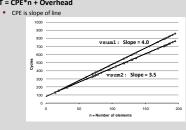
- int
- float
- double

■Operations

- Use different definitions of OP and IDENT
- **+** / 0
- * / 1

Cycles Per Element (CPE)

- Convenient way to express performance of program that operates on vectors or lists
- Length = n
- In our case: CPE = cycles per OP
- T = CPE*n + Overhead



Benchmark Performance

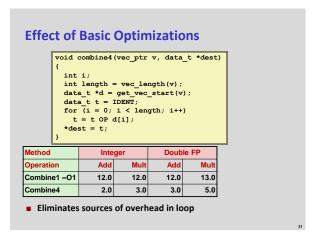
```
void combine1(vec_ptr v, data_t *dest)
                                                      Compute sum or
                                                      product of vector
     *dest = IDENT:
     for (i = 0; i < vec length(v); i++) {
                                                      elements
       get_vec_element(v, i, &val);
*dest = *dest OP val;
```

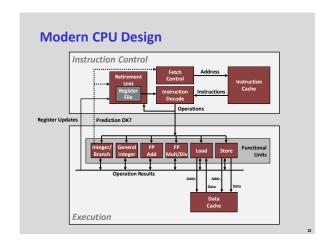
Method	Inte	ger	Doub	le FP
Operation	Add	Mult	Add	Mult
Combine1 unoptimized	29.0	29.2	27.4	27.9
Combine1 -01	12.0	12.0	12.0	13.0

Basic Optimizations

```
void combine4(vec_ptr v, data_t *dest)
  int length = vec length(v);
  data_t *d = get_vec_start(v);
 data_t t = IDENT;
for (i = 0; i < length; i++)</pre>
    t = t OP d[i];
  *dest = t;
```

- Move vec_length out of loop
- Avoid bounds check on each cycle
- Accumulate in temporary





Superscalar Processor

- Definition: A superscalar processor can issue and execute multiple instructions in one cycle. The instructions are retrieved from a sequential instruction stream and are usually scheduled dynamically.
- Benefit: without programming effort, superscalar processor can take advantage of the instruction level parallelism that most programs have
- Most CPUs since about 1998 are superscalar.
- Intel: since Pentium Pro

Nehalem CPU

- Multiple instructions can execute in parallel
 - 1 load, with address computation 1 store, with address computation
 - 2 simple integer (one may be branch)
 - 1 complex integer (multiply/divide)
 - 1 FP Multiply 1 FP Add
- Some instructions take > 1 cycle, but can be pipelined

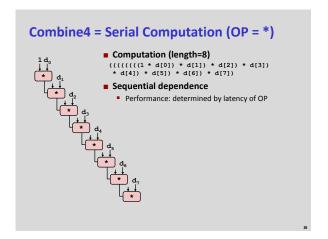
Instruction	Latency	Cycles/Issue
Load / Store	4	1
Integer Multiply	3	1
Integer/Long Divide	1121	1121
Single/Double FP Multiply	4/5	1
Single/Double FP Add	3	1
Single/Double FP Divide	1023	1023
	Load / Store Integer Multiply Integer/Long Divide Single/Double FP Multiply Single/Double FP Add	Load / Store 4 Integer Multiply 3 Integer/Long Divide 1121 Single/Double FP Multiply 4/5 Single/Double FP Add 3

x86-64 Compilation of Combine4

■ Inner Loop (Case: Integer Multiply)

.L519	:	# Loop:
imu	ll (%rax,%rdx,4	4), %ecx # t = t * d[i]
add	q \$1, %rdx	# i++
cmp	q %rdx, %rbp	# Compare length:i
jg	.L519	# If >, goto Loop

Combine4 2.0 3.0 3.0 5. Latency 1.0 3.0 3.0 5.	Method	Integer Double FP		le FP	
Latency 1.0 3.0 3.0 5.	Operation	Add	Mult	Add	Mult
	Combine4	2.0	3.0	3.0	5.0
Board	Latency Bound	1.0	3.0	3.0	5.0



Loop Unrolling

```
void unroll2a_combine(vec_ptr v, data_t *dest)
{
   int length = vec_length(v);
   int limit = length-1;
   data_t *d = get_vec_start(v);
   data_t x = IDENT;
   int i;
   /* Combine 2 elements at a time */
   for (i = 0; i < limit; i*=2) {
        x = (x OP d[i]) OP d[i*1];
   }
   /* Finish any remaining elements */
   for (; i < length; i*+) {
        x = x OP d[i];
   }
   *dest = x;
}</pre>
```

■ Perform 2x more useful work per iteration

Effect of Loop Unrolling

Method	Inte	Integer		le FP
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Latency Bound	1.0	3.0	3.0	5.0

- Helps integer multiply
 - below latency bound
 - Compiler does clever optimization
- Others don't improve. Why?
 - Still sequential dependency

x = (x OP d[i]) OP d[i+1];

Loop Unrolling with Reassociation

```
void unroll2aa_combine(vec_ptr v, data_t *dest)
{
    int length = vec_length(v);
    int limit = length-1;
    data_t *d = get_vec_start(v);
    data_t x = IDENT;
    int i;
    /* Combine 2 elements at a time */
    for (i = 0; i < limit; i+=2) {
        x = x OP (d[i] OP d[i+1]);
    }
    /* Finish any remaining elements */
    for (; i < length; i++) {
        x = x OP d[i];
    }
    *dest = x;
}</pre>
Compare to before

x = (x OP d[i]) OP d[i+1];
```

- Can this change the result of the computation?
- Yes, for FP. Why?

Effect of Reassociation

Method	Integer Double F		le FP	
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Unroll 2x, reassociate	2.0	1.5	1.5	3.0
Latency Bound	1.0	3.0	3.0	5.0
Throughput Bound	1.0	1.0	1.0	1.0

- Nearly 2x speedup for Int *, FP +, FP *
 - Reason: Breaks sequential dependency
 - x = x OP (d[i] OP d[i+1]);
 - Why is that? (next slide)

Reassociated Computation

```
x = x OP (d[i] OP d[i+1]);
```

- What changed:
 - Ops in the next iteration can be started early (no dependency)
- Overall Performance
- N elements, D cycles latency/op
- Should be (N/2+1)*D cycles:
- Measured CPE slightly worse for FP mult

Loop Unrolling with Separate Accumulators

```
void unroll2a_combine(vec_ptr v, data_t *dest) {
   int length = vec_length(v);
   int limit = length-1;
   data t *d = get_vec_start(v);
   data_t x0 = IDENT;
   data_t x1 = IDENT;
   int i;
   /* Combine 2 elements at a time */
   for (i = 0; i < limit; i+=2) {
      x0 = x0 OP d[i];
      x1 = x1 OP d[i+1];
   }
   /* Finish any remaining elements */
   for (; i < length; i++) {
      x0 = x0 OP d[i];
   }
   *dest = x0 OP x1;
}</pre>
```

■ Different form of reassociation

Effect of Separate Accumulators

Method	Inte	ger	Doub	le FP
Operation	Add	Mult	Add	Mult
Combine4	2.0	3.0	3.0	5.0
Unroll 2x	2.0	1.5	3.0	5.0
Unroll 2x, reassociate	2.0	1.5	1.5	3.0
Unroll 2x Parallel 2x	1.5	1.5	1.5	2.5
Latency Bound	1.0	3.0	3.0	5.0
Throughput Bound	1.0	1.0	1.0	1.0

- 2x speedup (over unroll2) for Int *, FP +, FP *
 - Breaks sequential dependency in a "cleaner," more obvious way

x0 = x0 OP d[i]; x1 = x1 OP d[i+1];

Unrolling & Accumulating

■ Idea

- Can unroll to any degree L
- Can accumulate K results in parallel
- L must be multiple of K

■ Limitations

- Diminishing returns
 - Cannot go beyond throughput limitations of execution units
- Large overhead for short lengths
 - Finish off iterations sequentially

Unrolling & Accumulating: Double *

■ Case

- Intel Nehalem
 - Double FP Multiplication
 - Latency bound: 5.00. Throughput bound: 1.00

	FP*			U	nrolling	Factor L			
	K	1	2	3	4	6	8	10	12
	1	5.00	5.00	5.00	5.00	5.00	5.00		
rs	2		2.50		2.50		2.50		
Accumulators	3			1.67					
Inc	4				1.25		1.25		
nn	6					1.00			1.19
Acc	8						1.02		
	10							1.01	
	12								1.00

Unrolling & Accumulating: Int +

■ Case

- Intel Nehalem
- Integer addition
- Latency bound: 1.00. Throughput bound: 1.00

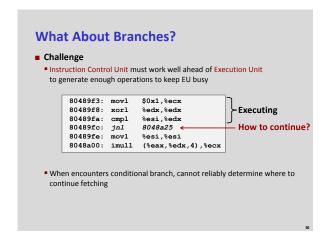
	FP*			U	Inrolling	Factor L			
	K	1	2	3	4	6	8	10	12
	1	2.00	2.00	1.00	1.01	1.02	1.03		
rs	2		1.50		1.26		1.03		
Accumulators	3			1.00					
lηι	4				1.00		1.24		
un:	6					1.00			1.02
Acc	8						1.03		
-	10							1.01	
	12								1.09

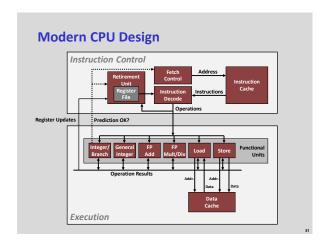
Achievable Performance

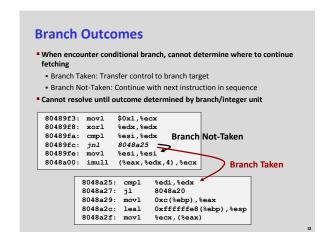
Method	Inte	ger	Doub	le FP
Operation	Add	Mult	Add	Mult
Scalar Optimum	1.00	1.00	1.00	1.00
Latency Bound	1.00	3.00	3.00	5.00
Throughput Bound	1.00	1.00	1.00	1.00

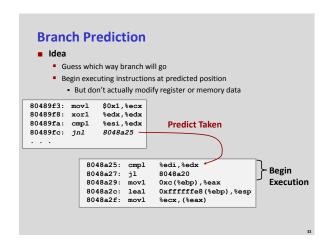
- Limited only by throughput of functional units
- Up to 29X improvement over original, unoptimized code

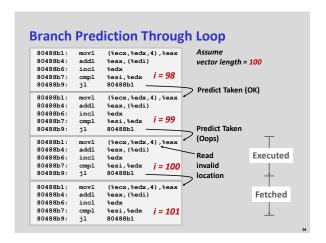
.atency Bound 1.00 3.00 3.00 5.00 /Fhroughput Bound 1.00 1.00 1.00 1.00 /ec Throughput 0.25 0.50 0.50 0.50	Wethod	Integer		Double F	P
/ector Best 0.25 0.53 0.53 0.57 .atency Bound 1.00 3.00 3.00 5.00 Throughput Bound 1.00 1.00 1.00 1.00 /ec Throughput 0.25 0.50 0.50 0.50 3ound Make use of SSE Instructions Parallel operations on multiple data elements	Operation	Add	Mult	Add	Mult
Attency Bound 1.00 3.00 3.00 5.00	calar Best	1.00	1.00	1.00	1.00
Make use of SSE Instructions Parallel operations on multiple data elements	Vector Best	0.25	0.53	0.53	0.57
Vec Throughput 0.25 0.50 0.50 0.50 Make use of SSE Instructions Parallel operations on multiple data elements	Latency Bound	1.00	3.00	3.00	5.00
Make use of SSE Instructions Parallel operations on multiple data elements	Throughput Bound	1.00	1.00	1.00	1.00
Parallel operations on multiple data elements	Vec Throughput Bound	0.25	0.50	0.50	0.50

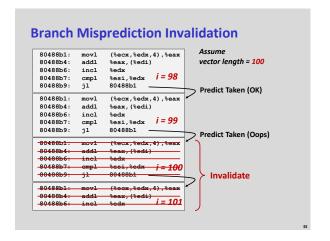


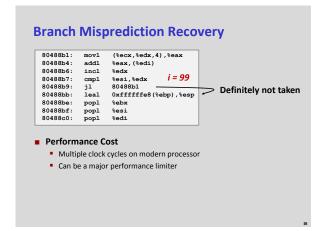












Branch Prediction: Bad News

■ Some program branches are inherently unpredictable

Partial solution: write code to be compiled to conditional

E.g., if based on input data, binary search tree, etc.

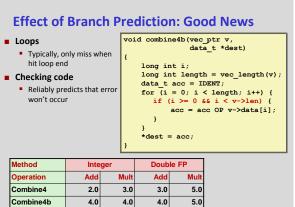
Indirect jumps are also often hard to predict

■ These can be a major performance bottleneck

Textbook gives min/max and mergesort examples

Misprediction penalty is typically 10-20 cycles

• For GCC: use math and ? : instead of if



Summary: Getting High Performance

Watch out for hidden algorithmic inefficiencies

 Watch out for optimization blockers: procedure calls & memory references
 Look carefully at innermost loops (where most work is done)

Make code cache friendly (Covered later in course)

Good compiler and flagsDon't do anything stupid

■ Tune code for machine

Write compiler-friendly code

Exploit instruction-level parallelism
 Avoid unpredictable branches

moves