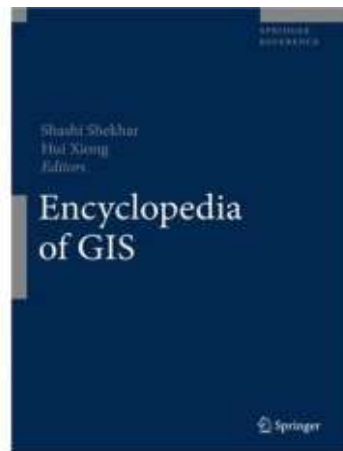
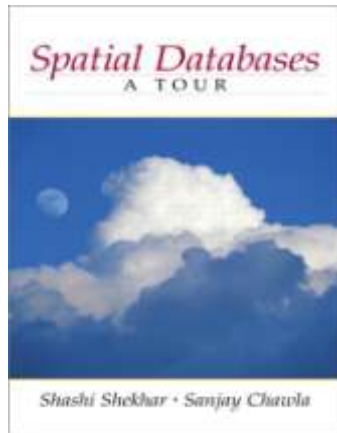


# *Spatio-temporal Data Mining for Environmental Sciences*

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# Acknowledgements

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## ■ **Collaborators (Env. Scientists):**

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## ■ **Sponsors:**

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# Spatio-Temporal Data Analysis



A Smarter Planet



ORACLE  
SPATIAL



Microsoft  
Virtual Earth



Recently having attention in Industry and Academia



# Outline

---

- Spatial and Spatio-temporal Data Mining
- Environmental Science
- Flow Anomalies
- Gaps, Open Problems

# Spatial and Spatio-temporal Data Mining



## 1. What is it?

- ① Identifying interesting, useful, non-trivial **patterns**
- ② in large **spatial** or **spatio-temporal** datasets

## 2. Why is it important ?

- ① Potential of insights to improve human lives
  - Environment: How is Earth system changing? Consequences for humans?
  - Public health: Where are cancer clusters? Environmental reasons?
  - Public safety: Where are hotspots of (env.) crime? Why?
- ② However,  $(d/dt) (\text{Spatial Data Volume}) \gg (d/dt) (\text{Number of Human Analysts})$ 
  - Need automated methods to mine patterns from spatial data
  - Need tools to amplify human capabilities to analyze spatial data

# Spatial Data Mining (SDM)

---

## 1. The process of discovering

- ① interesting, useful, non-trivial patterns
  - patterns: non-specialist
  - exception to patterns: specialist
- ② from large **spatial** datasets

## 2. Spatial pattern families

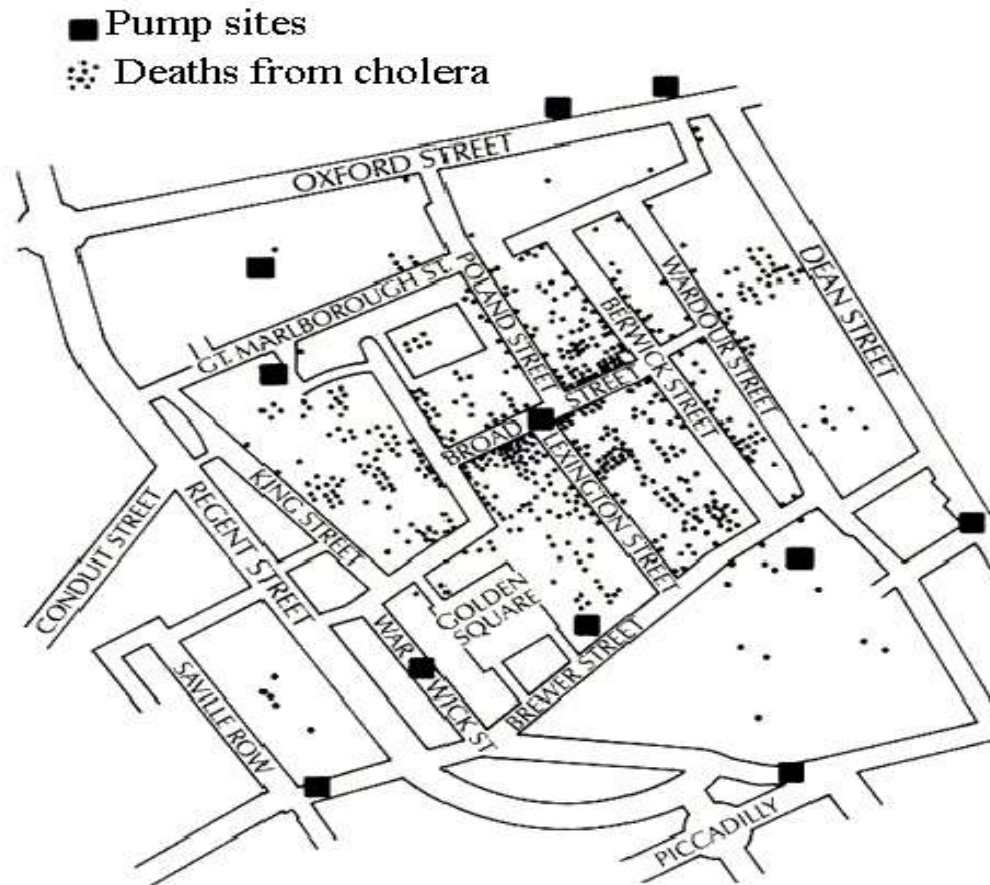
- ① Hotspots, Spatial clusters
- ② Spatial outlier, discontinuities
- ③ Co-locations, co-occurrences
- ④ Location prediction models
- ⑤ ...

# Pattern Family: Hotspots, Spatial Cluster

---

## The 1854 Asiatic Cholera in London

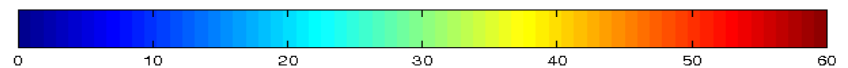
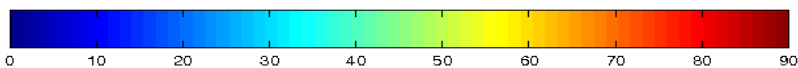
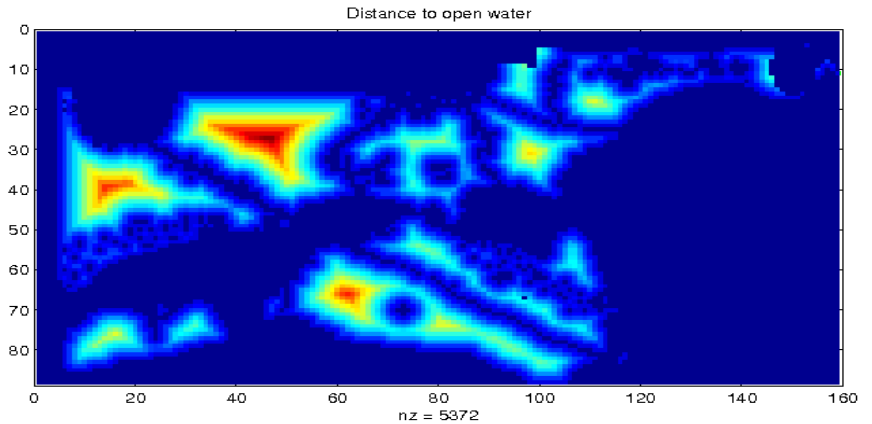
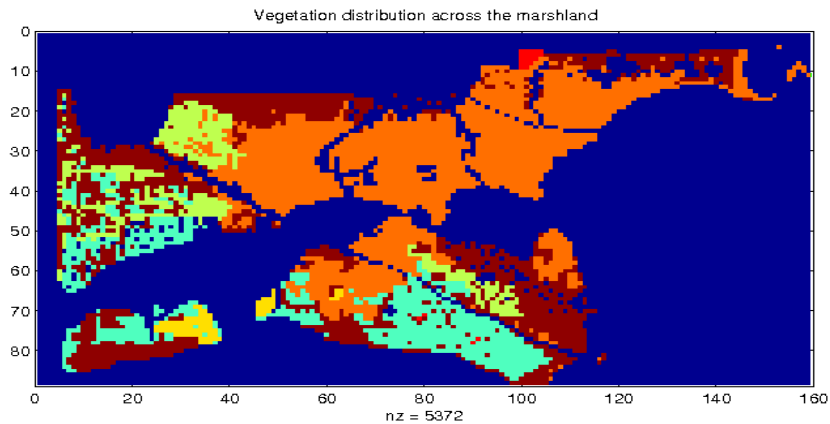
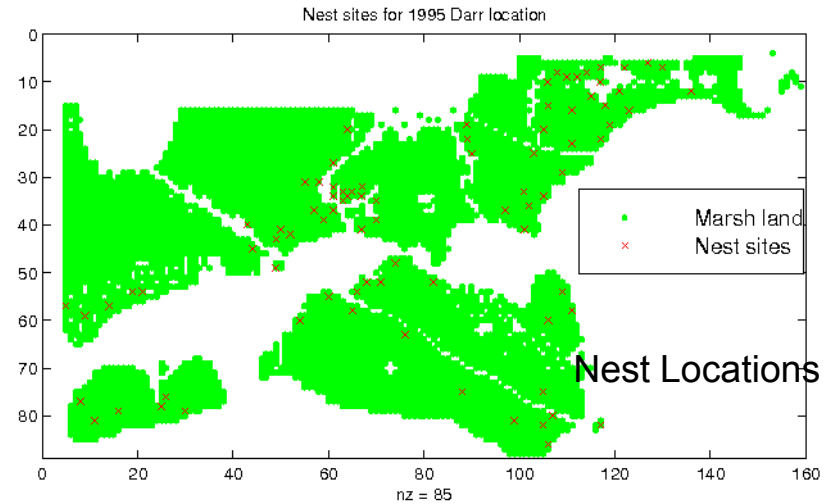
Near Broad St. water pump except a brewery



# Pattern Family : Predictive Models

## Location & Direction Prediction:

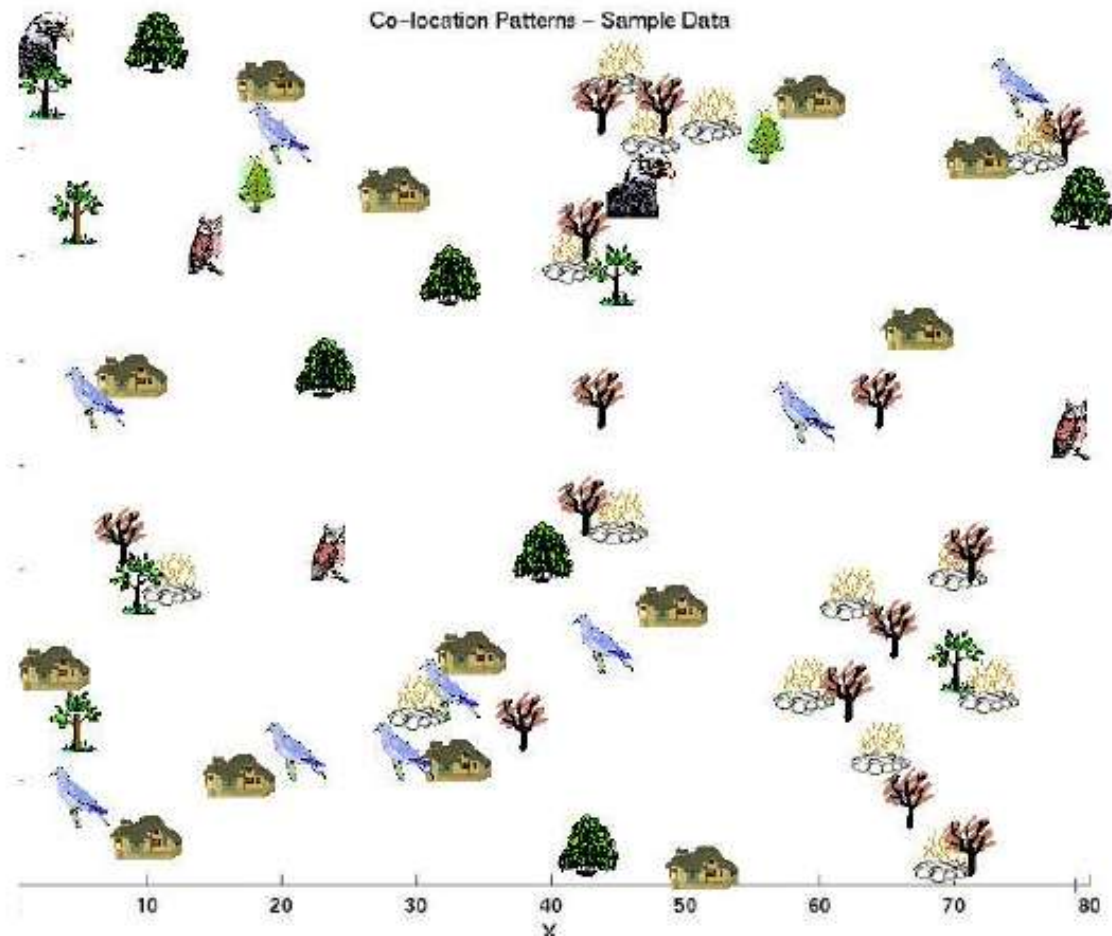
Predict Bird Habitat Prediction  
Using environmental variables





# Pattern Family : Co-locations/Co-occurrence

- ⑩ Given: A collection of different types of spatial events
- ⑩ Find: Co-located subsets of event types



Answers:



and



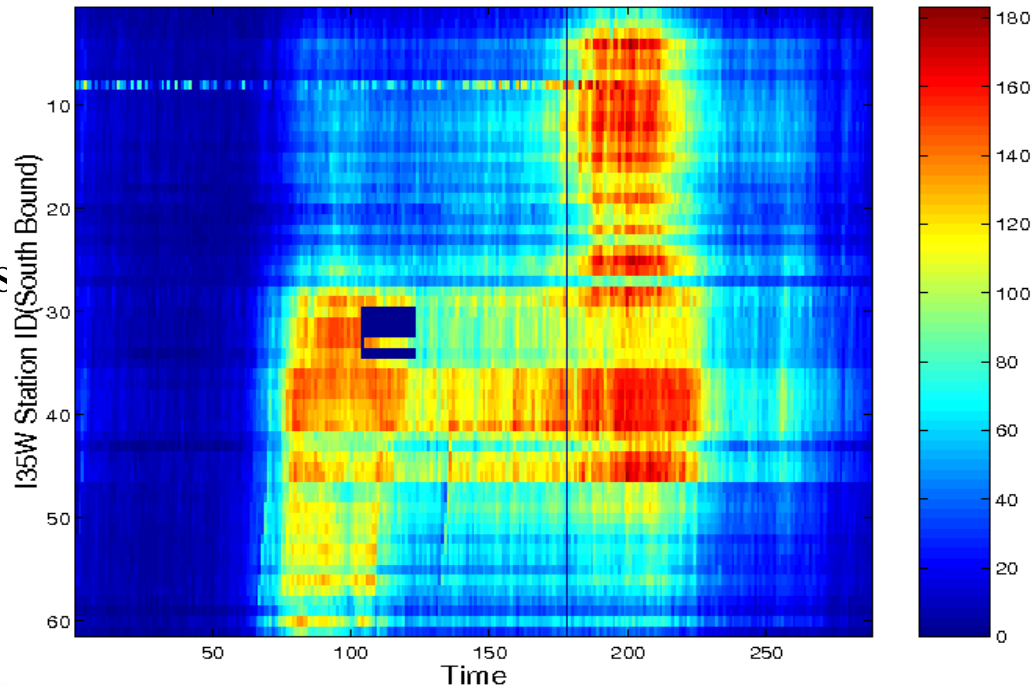
# Pattern Family: Spatial Anomalies

## Spatial Anomalies

- ① Traffic Data in Twin Cities
- ② Abnormal Sensor Detections
- ③ Spatial and Temporal Outliers



Average Traffic Volume(Time v.s. Station)

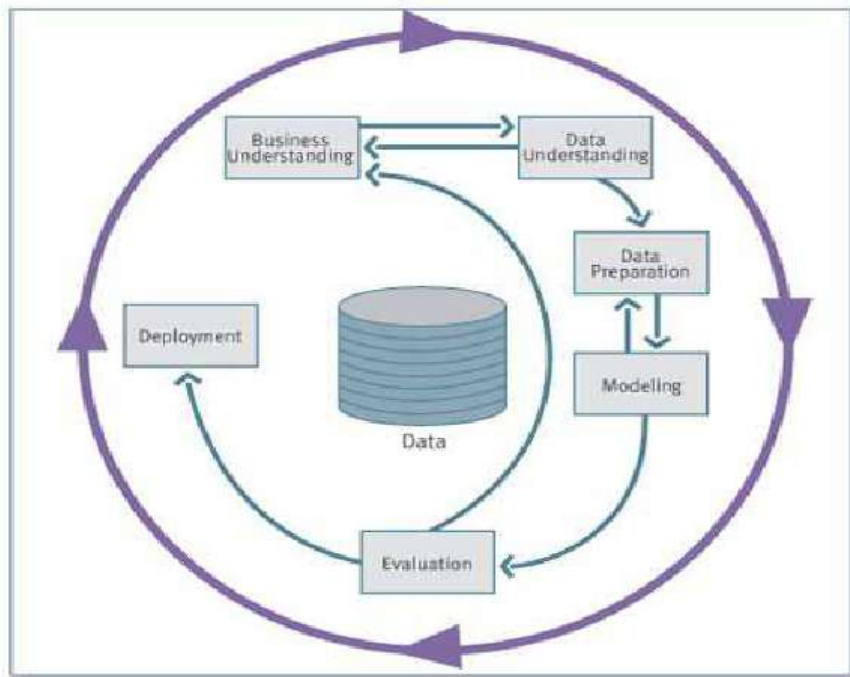


# Life Cycle of Data Mining

---

## CRISP-DM (CRoss-Industry Standard Process for DM)

- ① Application/Business Understanding
- ② Data Understanding
- ③ Data Preparation
- ④ Modeling
- ⑤ Evaluation
- ⑥ Deployment



Phases of CRISP-DM

Is CRISP-DM adequate for Spatial Data Mining?

[1] CRISP-DM URL:  
<http://www.crisp-dm.org>

# Outline

---

- Spatial and Spatio-temporal Data Mining
- Environmental Science
- Flow Anomalies
- Gaps, Open Problems

# *Environment, Environmental Science*

---

## ⑩ **Environment**

- ① surroundings; milieu
- ② aggregate of surrounding things, conditions, or influences;.
- ③ Ecology . the air, water, minerals, organisms, and all other external factors surrounding and affecting a given organism at any time.
- ④ Social and cultural forces that shape the life of a person or a population

## **Q? What is the relationship to spatial / spatio-temporal analysis?**

It allow inclusion of context, i.e. surrounding.

## ⑩ **Environmental Science**

- ① study of the interactions among the physical, chemical and biological components of the environment
- ② branch of science concerned with the physical, chemical, and biological conditions of the environment and their effect on organisms.

# Examples of Environmental Sciences

---

## ⑩ **Environmental chemistry:**

- ⑩ Soil, water, air pollution; multi-phase transport, fate; impact on species, geology
- ⑩ Study of chemical alterations in the environment.

## ⑩ **Atmospheric sciences:**

- ⑩ meteorology, greenhouse gas phenomena, airborne contaminant dispersion, ...
- ⑩ Global warming: atmospheric circulation, air-borne chemicals and their reactions, carbon dioxide fluxes from life-forms, atmospheric dynamics, etc.

## ⑩ **Geosciences, hydrology, oceanography:**

- ⑩ environmental geology, environmental soil science, volcanic phenomena, surface runoff, sediment transport, water turbidity, ...

## ⑩ **Ecology:**

- ⑩ study of organisms and their interactions with each other and their environment

## ⑩ **Env. Health, Env. Physiology, ...**

## ⑩ **Env. Justice, Env. Criminology**

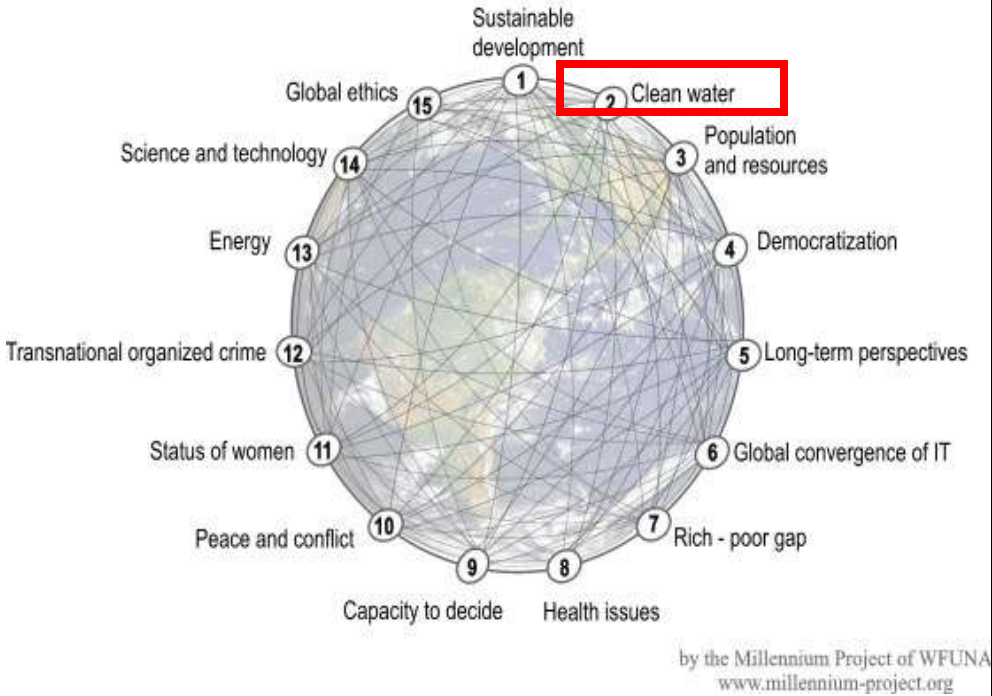
## ⑩ **Env. Engineering**

## ⑩ **Env. Psychology, Env. Sociology**

## ⑩ **...**

# Water Quality

## 15 Global Challenges facing humanity



## What's in our Water?



Recent studies found presence of pharmaceutical drugs in drinking water of many U.S. Cities

Source: **New York Times (April 3, 2007)**  
(<http://www.nytimes.com/2007/04/03/science/earth/03water.html>)

- **By 2025**, 1.8 billion people could be living in water scarce areas
  - **Today**, 750 million people live below the water-stress threshold of 1.7 K cubic meters per person
- Source: WFUNA, 15 Global Challenges



# Environmental Questions

---

## 1. General Public

- ① Is water safe for drinking, swimming ?
- ② Where are air quality warning?

## 2. Drinking Water Manager

- ① Is incoming water safe for water plant (reverse osmosis filters)?
- ② Is there a change in contaminants today (compared with recent days)?

## 3. Environmental Scientist

- ① Transport: Where will a contaminant go?
- ② Fate: What is the fate of a contaminant ?
- ③ Are there any new processes occurring in the water bodies?

## 4. Environmental Forensics

- ① Where did contaminant come from ?
- ② What are hotspots and hot moments?

## 5. Policy

- ① Compare policy options on environmental impact and social good.?
- ② How to communicate environmental decision to all stakeholders?

## 6. Environment Protection Agency

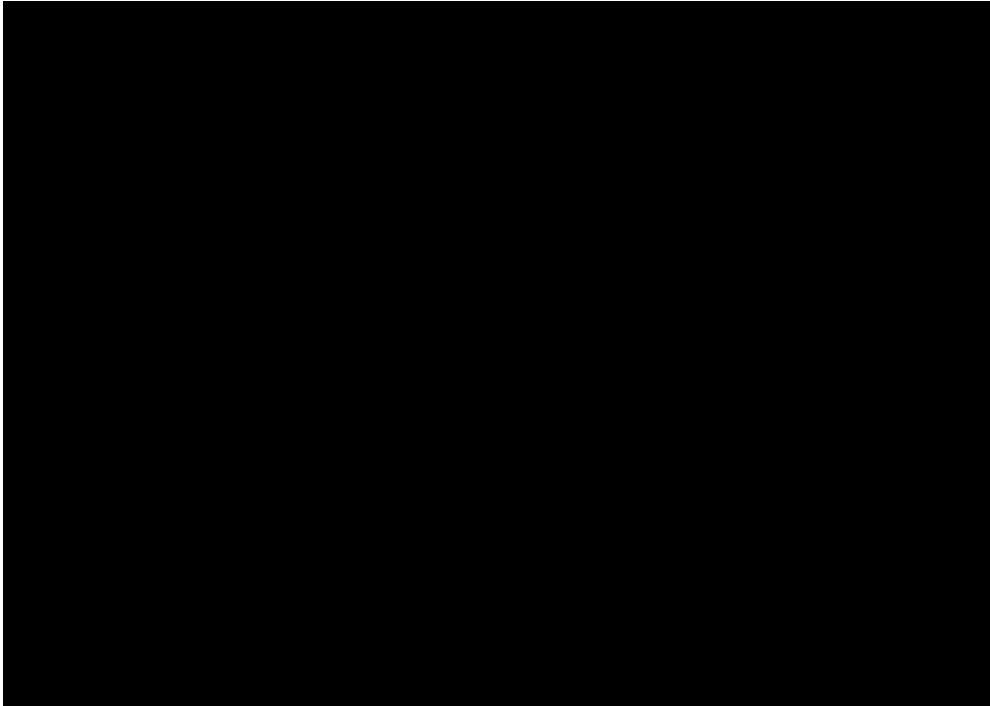
- ① What will be the impact on environment of a proposed change?





### ES Domain Questions:

- Where do various contaminants go?
- Where did the contamination come from?



Path of Pollutant within the Environment  
(Source: Schnoor, Environmental Modeling, 1996)



Gulf of Mexico



# Datasets

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## Data Sources:

- Hydrology Information Systems, CUAHSI
- United States Geological Survey

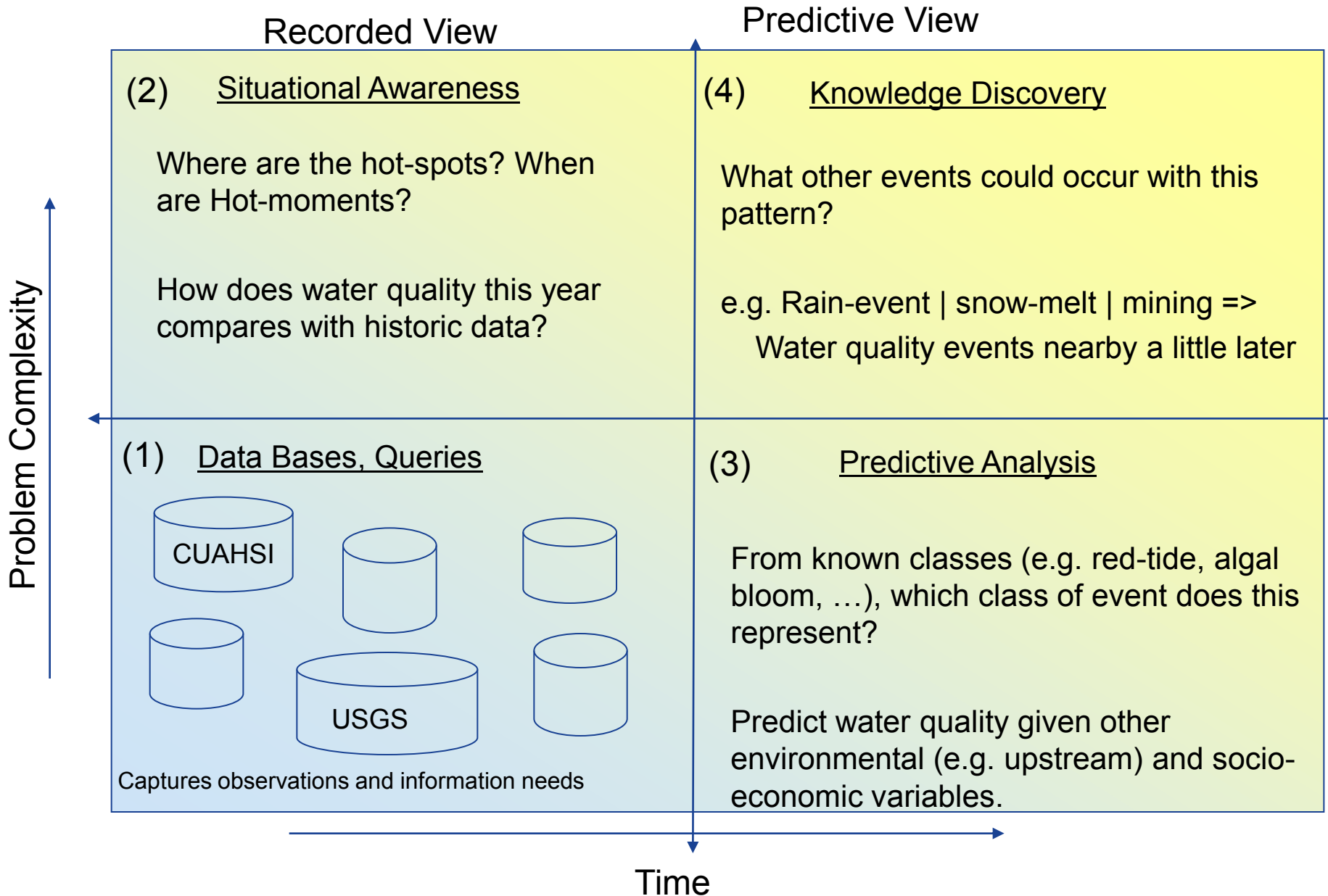
## Data Characteristics (HIS/USGS)

- > 1.75 Million Locations
- > 342 Million Time Instants
- > 15K Measured Variables
  - Turbidity
  - Dissolved Oxygen
  - Nitrate
  - Etc.



Hydrology Measurement Sites in US  
(Source: HIS/USGS)

# Environmental Science: Data Analysis



# Outline

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- Spatial and Spatio-temporal Data Mining
- Environmental Science
- Flow Anomalies

## **Key Concepts**

**Problem Statement**

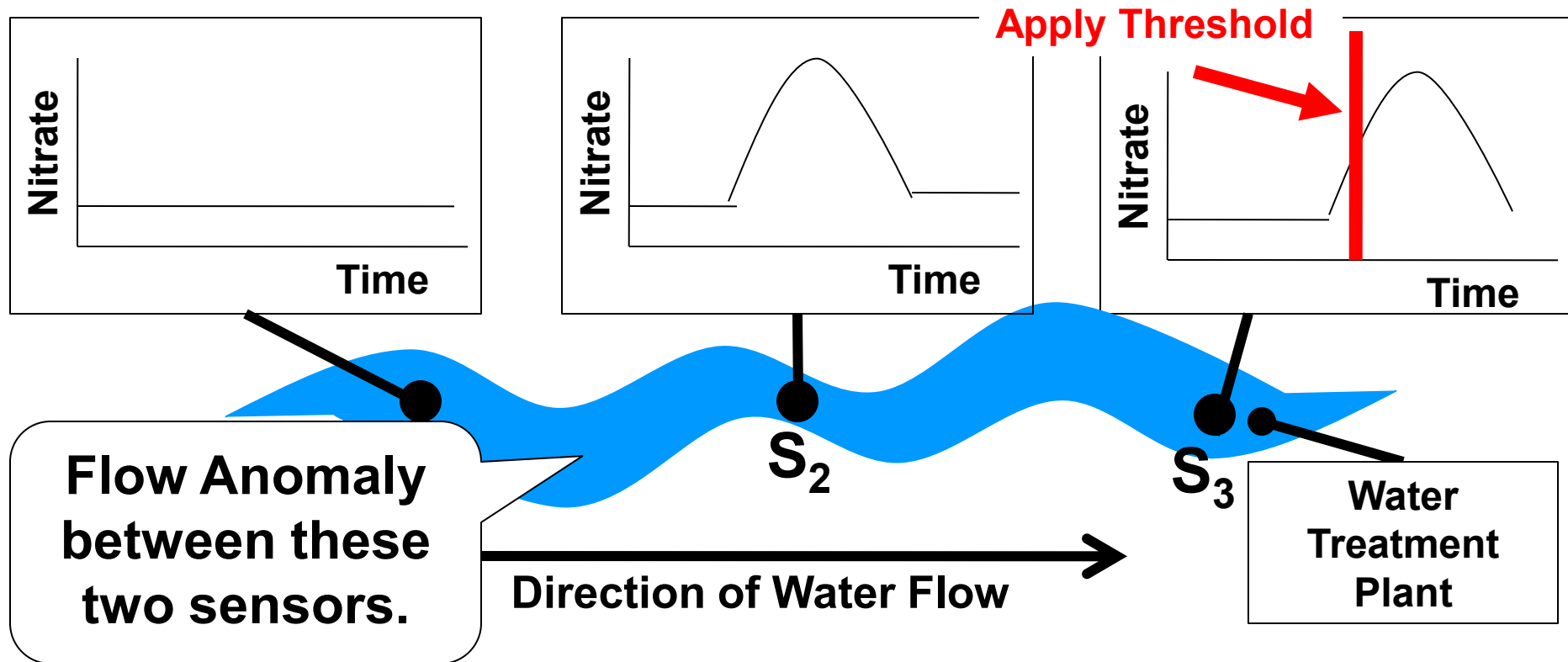
**Contributions**

**Analytical Evaluation**

**Experimental Evaluation**

- Gaps, Open Problems

# Motivation – Detailed Example



## Two Use Cases:

- At the water treatment plant, when should it turn off the water supply from the river?
- **Where is the source of the contaminant?**

# *Domain Example of a Flow Anomaly*

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Chronicle / Kurt Rogers

(Source: <http://www.sfgate.com/cgi-bin/news/oilspill/busan>)

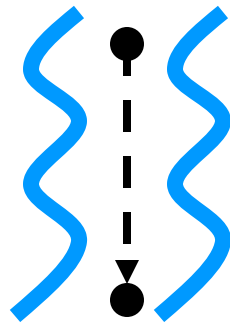
Notice that a contaminant event may **not** flow as a single contiguous unit.

Other Applications:

- Atmospheric Monitoring
- Pipeline Systems
- Transportation Networks

# Concept: Transient Flow Anomaly

- **Transient Flow Anomaly (tFA)** is where the difference between the neighboring observations across each sensor is larger than the given error threshold,  $\Theta_e$
- **Ex.** Suppose  $\Theta_e = 10$



$t =$	1	2	3	4
$TT [t] =$	1	1	1	1
$f(st_1) =$	10	20	30	40
$f(st_2) =$	0	90	25	85
$tFA [t] =$	1	0	1	-

A tFA may represent a single time unit of a blob in an oil spil.

# Concept: Persistent Flow Anomaly

- **Persistent Flow Anomaly (pFA)**, is when the first and last are tFAs and the fraction of tFAs and time slots within a period satisfies the persistent threshold,  $\Theta_p$
- Ex. Suppose  $\Theta_e = 10$  and  $\Theta_p = 0.5$

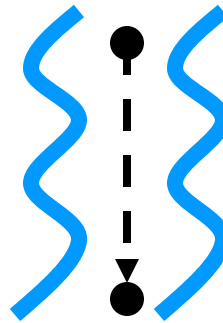
For a pFA of  $s = 1$  and  $e = 3$ ,

pFA [1,2,3] exists because

$$A[1] = 1 \ \& \ A[3] = 1 \ \& \ 2/3 \geq 0.5$$

Thus, a pFA pattern is 1-3

A pFA may represent a single blob or chunk in an oil spill.



$t =$	1	2	3	4
$TT [t] =$	1	1	1	1
$f(st_1) =$	10	20	30	40
$f(st_2) =$	0	90	25	85
$tFA [t] =$	1	0	1	-

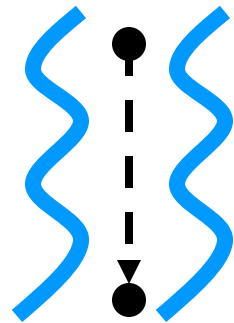
Note: A pFA is an *algebraic aggregate function*



# Concept: Dominant Persistent Flow Anomaly

## Anomaly

1. A dominant persistent Flow Anomaly, *dpFA*, is a pFA that has the largest possible number of IPs and is not a subset of any other dpFA.
2. Ex, Suppose  $\Theta_e = 10$  and  $\Theta_p = 0.5$



FA 1-5

t =	1	2	3	4	5	6
TT [t] =	1	1	1	1	1	1
f(st <sub>1</sub> ) =	10	20	30	40	50	60
f(st <sub>2</sub> ) =	0	90	25	85	45	90
tFA [t] =	1	0	1	0	1	-

Period 1-5 is a dpFA because it has the largest number of IPs and is not a subset of any other dpFA.

Periods 1-3 and 3-5 are not dpFAs because they are subsets of the dpFA of 1-5.

A dpFA may represent an entire oil event.

Note: A dpFA is a *holistic aggregate function*

# Outline

---

- Spatial and Spatio-temporal Data Mining
- Environmental Science
- Flow Anomalies
  - Key Concepts**
  - Problem Statement**
  - Contributions**
  - Analytical Evaluation**
  - Experimental Evaluation**
- Gaps, Open Problems

# Problem Statement

---

## ■ Given

- Two stations,  $st_1$  and  $st_2$
- Direction of flow between the  $st_1$  and  $st_2$  stations
- An upstream of contiguous set of Instant Pairs,  $IP$ , at time intervals  $t = 1 \dots n$  where  $n$  is the length of the time series for the  $s_1$  sensor
- The travel time,  $TT[t]$ , between the  $st_1$  and  $N(st_1)$  stations at every  $t$
- An error threshold  $\Theta_e$  and a persistent threshold  $\Theta_p$

## ■ Find

- All dominant persistent Flow Anomalies (dpFAs)

## ■ Objective

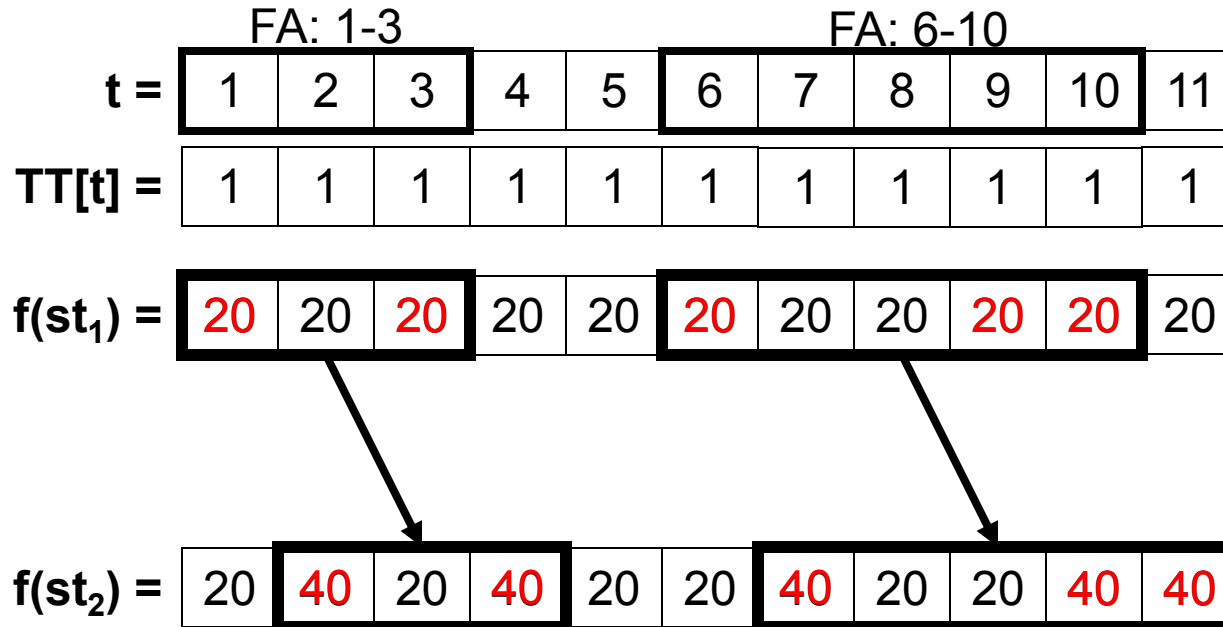
- Minimize computation time

## ■ Constraints

- A single directional flow between sensors
- Correct and complete

# Problem Statement: Example

Input:



$$\Theta_p = .60$$

$$\Theta_e = 0$$

**Output:** dpFAs of 1-3 and 6-10

Note: period 1-10 is NOT a dpFA because it does not satisfy the persistence threshold

Key:

Red Font – tFA

Black Box – dpFA

# Challenges and Related Work

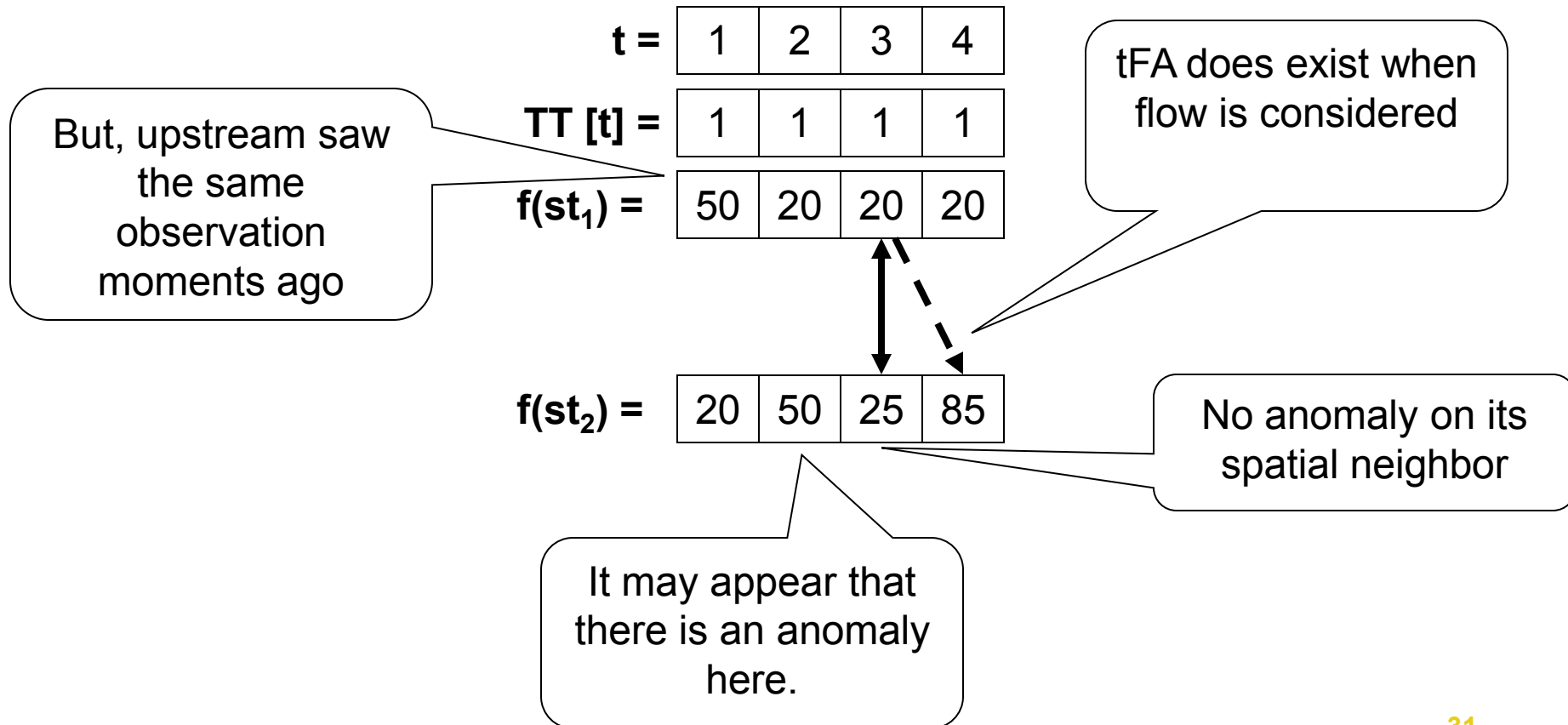
---

- **A single dpFA pattern may consist of subsets that may not be anomalies**
  - Violates Dynamic Programming Principle of having optimal substructure
    - String Matching [Lee, VLDB, '07], [Amir, J. Algorithms, '97]
    - Time Series [Keogh, KDD, '99]
  - Due to the fact that a pFA is an *algebraic aggregate function* that must satisfy a persistent threshold,  $\Theta_p$
  
- **The size of the dpFAs may not be known in advance**
  - Fixed Window Methods [Bulut, ICDE, '05],[Chen, ASIAN, '05], [Sakurai, SIGMOD, '05],[Sayal, HP, '04]

# Challenges and Related Work – Contd.

- **Outlier Detection may not find Transient FA [Knorr & Ng, KDD '97] [Shekhar et al., KDD '01]**

- Ex. Suppose  $\Theta_e = 10$



# Outline

---

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- Flow Anomalies
  - Key Concepts**
  - Problem Statement**
  - Contributions**
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# Our Contributions

---

- **Define Flow Anomalies (FA) and the FA Mining Problem**
- **New interest measures to discover and mine FAs**
- **Methods**
  - Naïve Approach
  - A Smart Window Enumeration and Evaluation of persistent Thresholds (SWEET) Approach
    - A Smart Counter Design Decision
    - A Pruning Strategy
  - An Expanded Ranges Index (SWEET-ER)
- **Analytical Evaluation**
- **Experimental Evaluation**
  - Synthetic and Real Datasets



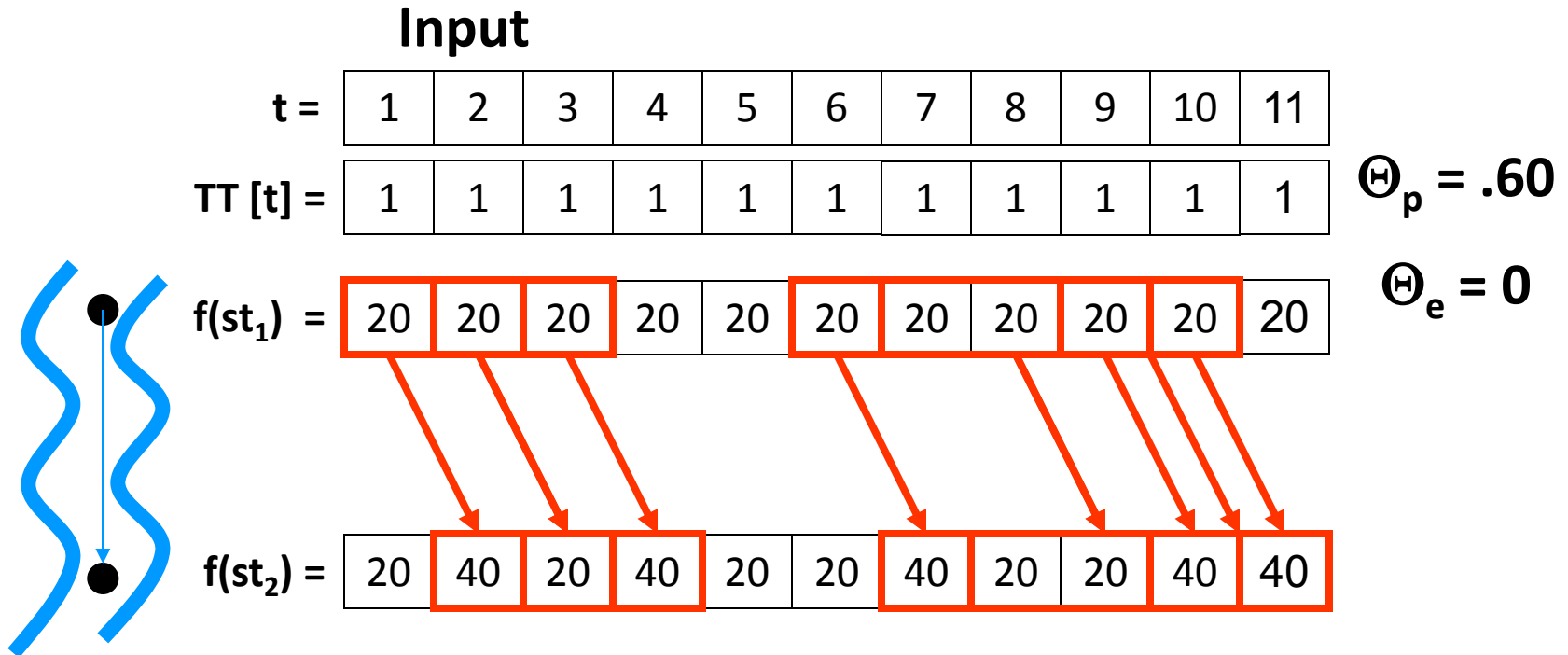
# *Naïve Approach*

---

- **In general, need to check every time period size to determine if it is anomalous or not.**
  - Utilize the travel time to identify the anomalous time periods
  - Exhaustive search for all possible time period sizes
    - Evaluate each period for number of tFAs and if it satisfies the persistent threshold
  - Example next slide

# Naïve Approach

## Example



**persistent Flow Anomalies**

**Size 1:** 1-1, 3-3, 6-6, 9-9, 10-10

**Size 2:** 9-10

**Size 3:** 1-3

**Size 4:** None

**Size 5:** 6-10

Can we stop?

**Size 6:** None

**Size 7:** None

**Size 8:** None

**Size 9:** None

**Size 10:** None

**dominant persistent Flow Anomalies:**

1-3, 6-10

# Analytical Evaluation

## Computational Costs

---


Complexity: (Phase 1 costs + Phase 2 costs)

	Worst Case
Naïve	$n^3 + p^2$

- **n is the total number of time slots in the dataset**
- **t is the number of tFAs found in the dataset and  $t \leq n$**
- **p is the number of pFAs found in the dataset and  $t \leq p \leq t^2$**

# Search Space

---



$t =$	1	2	3	4	5	6	7	8	9	10	11
$TT[t] =$	1	1	1	1	1	1	1	1	1	1	1
$f(st_1) =$	20	20	20	20	20	20	20	20	20	20	20
$f(st_2) =$	20	40	20	40	20	20	40	20	20	40	40

$$\Theta_p = .60$$

$$\Theta_e = 0$$

Key:

Red Font – tFA

**Examine all possible periods in this example in a Matrix and a Graph**  
**Observed THREE key insights to improve overall efficiency**

# Search Space: Matrix

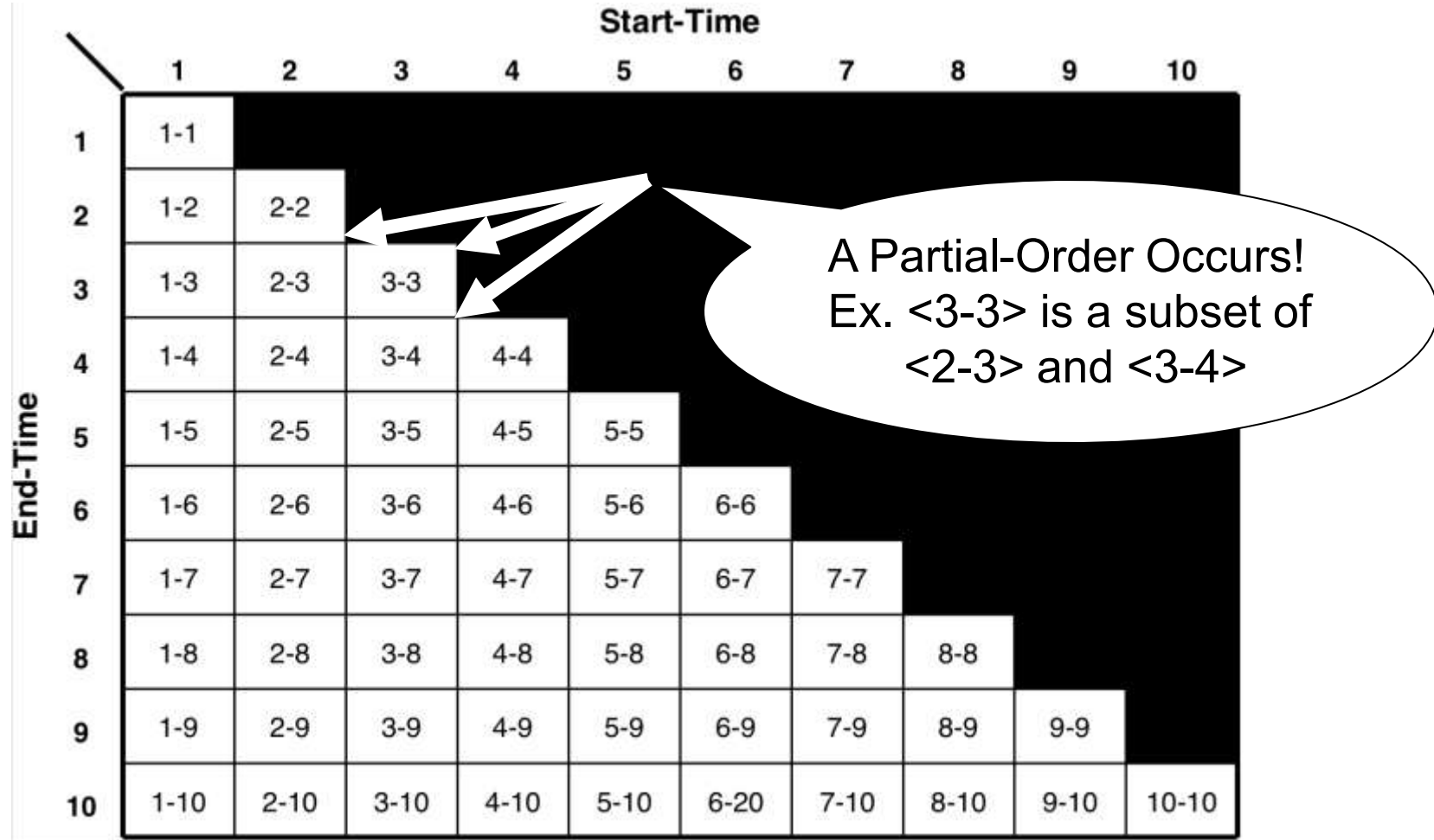
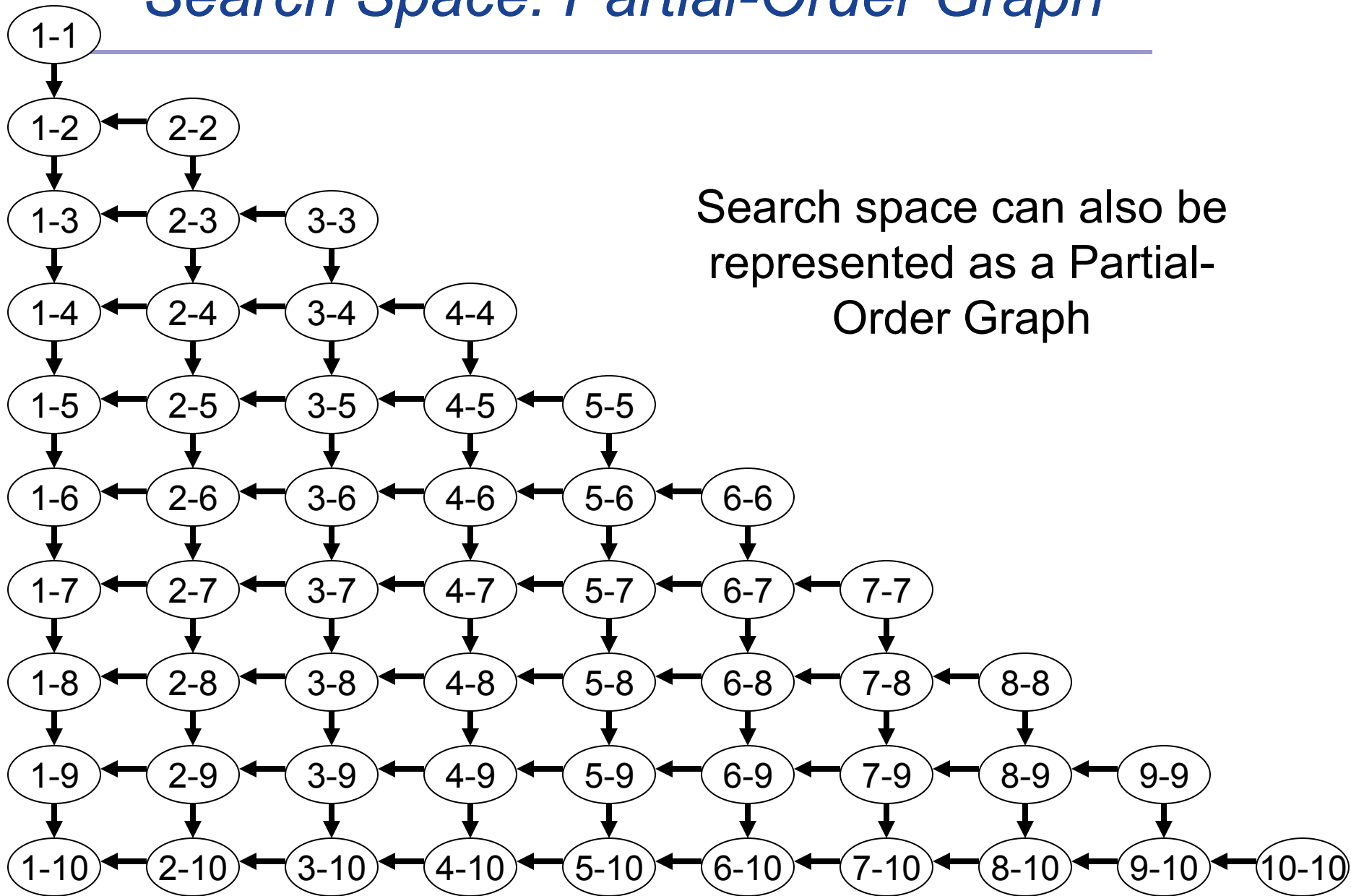


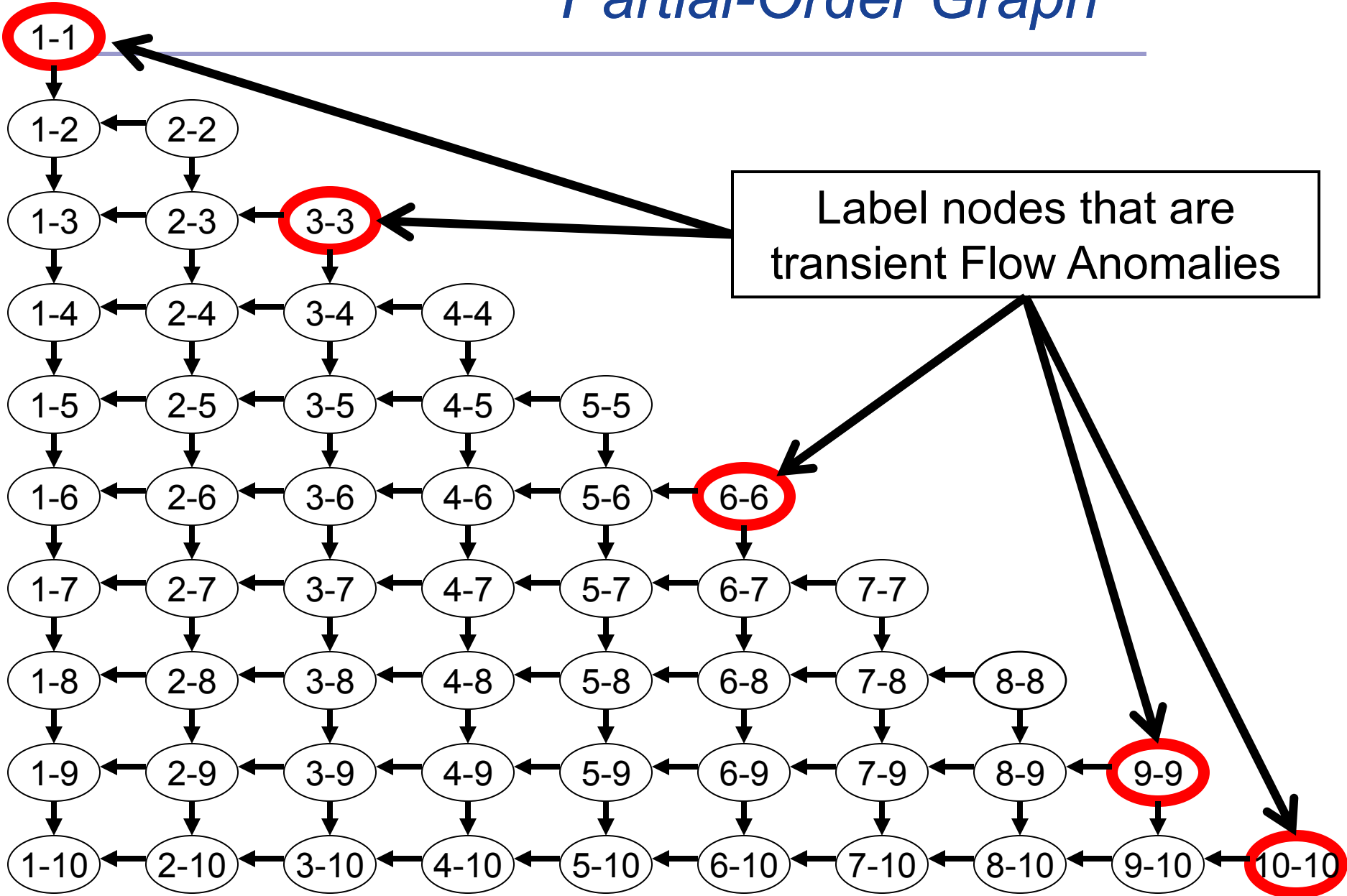
Illustration of All Candidate Time Intervals

# Search Space: Partial-Order Graph

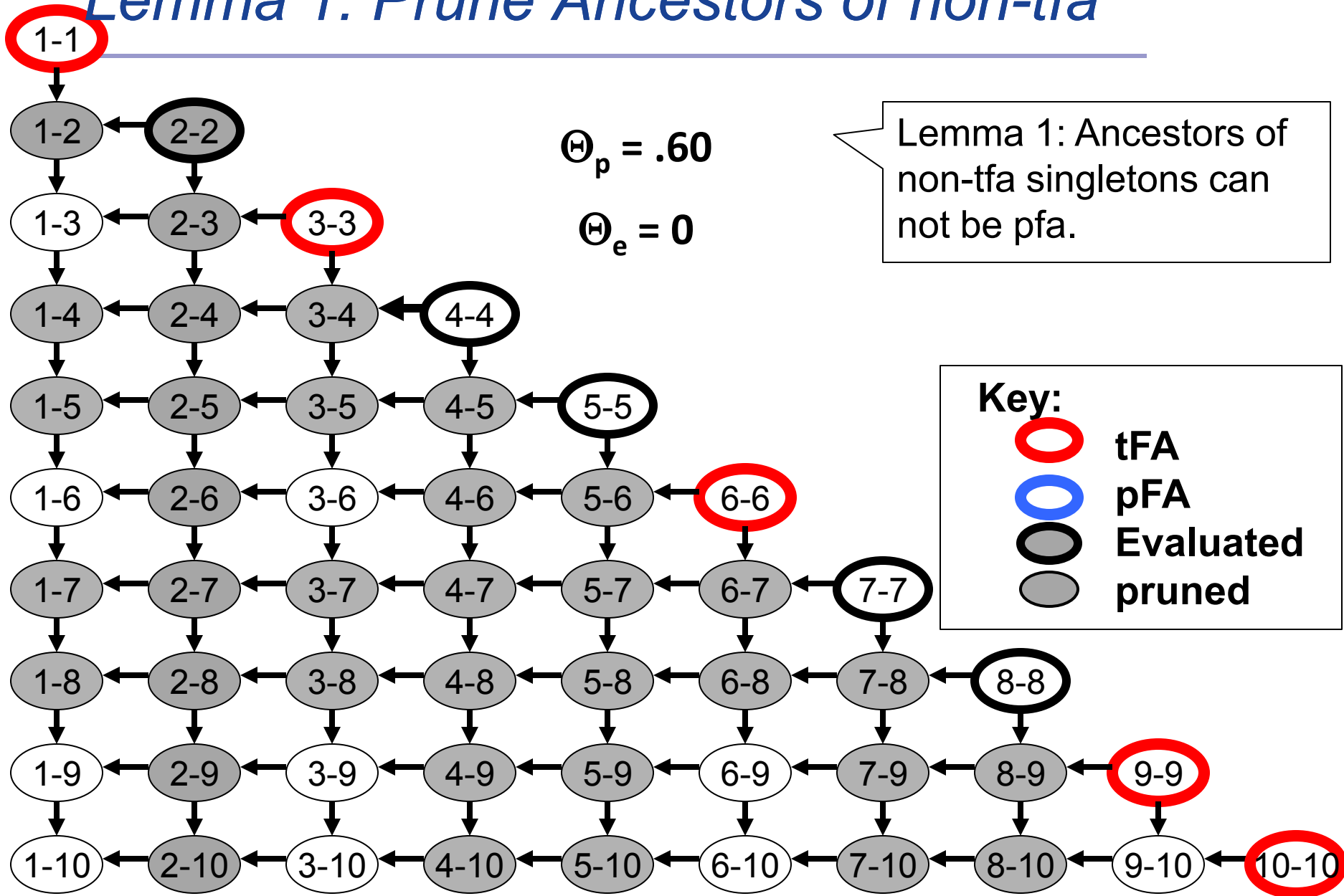


Search space can also be represented as a Partial-Order Graph

# Partial-Order Graph



# Lemma 1: Prune Ancestors of non-tfa

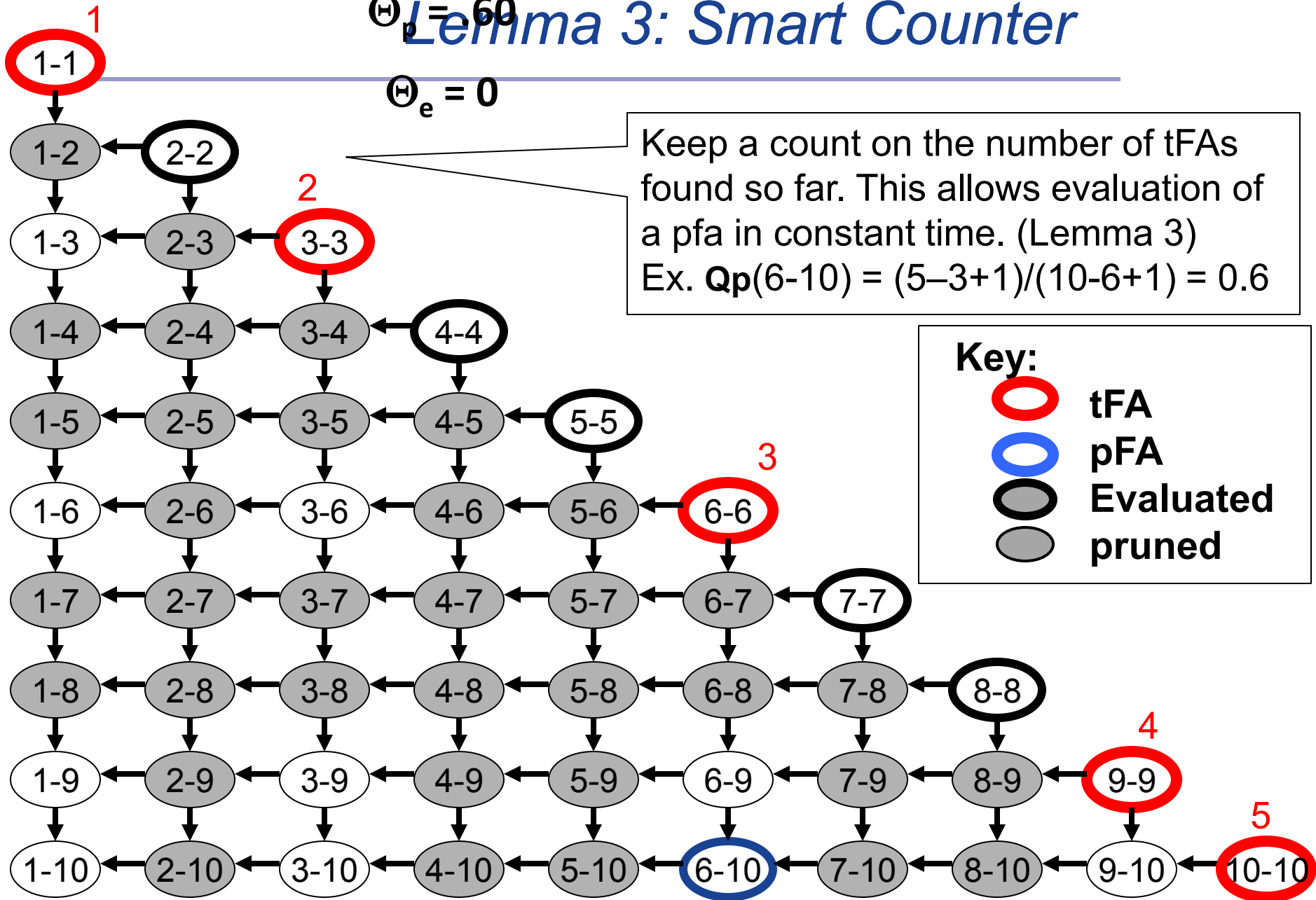




# $\Theta_p = 60$ Lemma 3: Smart Counter

$$\Theta_e = 0$$

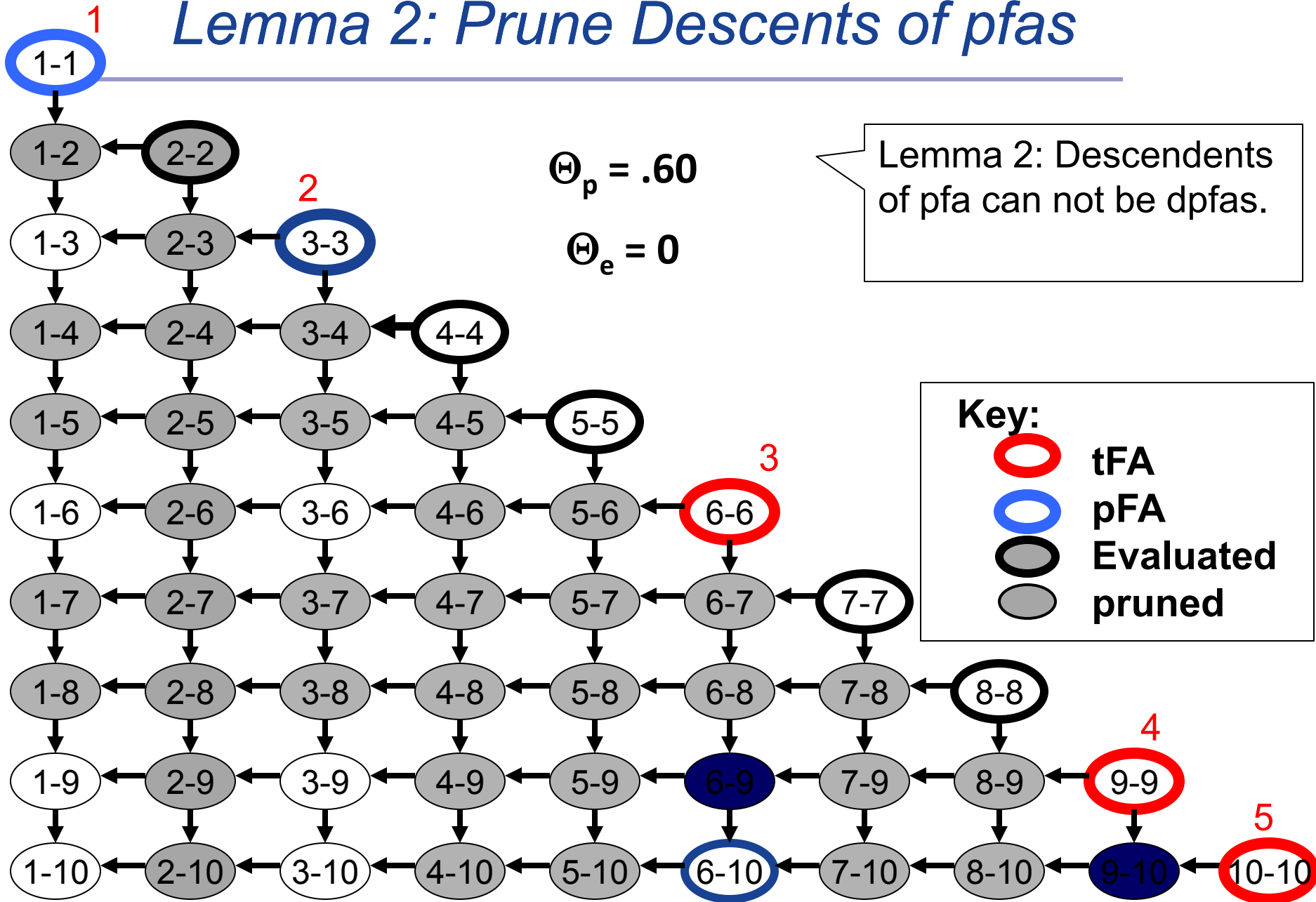
Keep a count on the number of tFAs found so far. This allows evaluation of a pfa in constant time. (Lemma 3)  
 Ex.  $Qp(6-10) = (5-3+1)/(10-6+1) = 0.6$



**Key:**

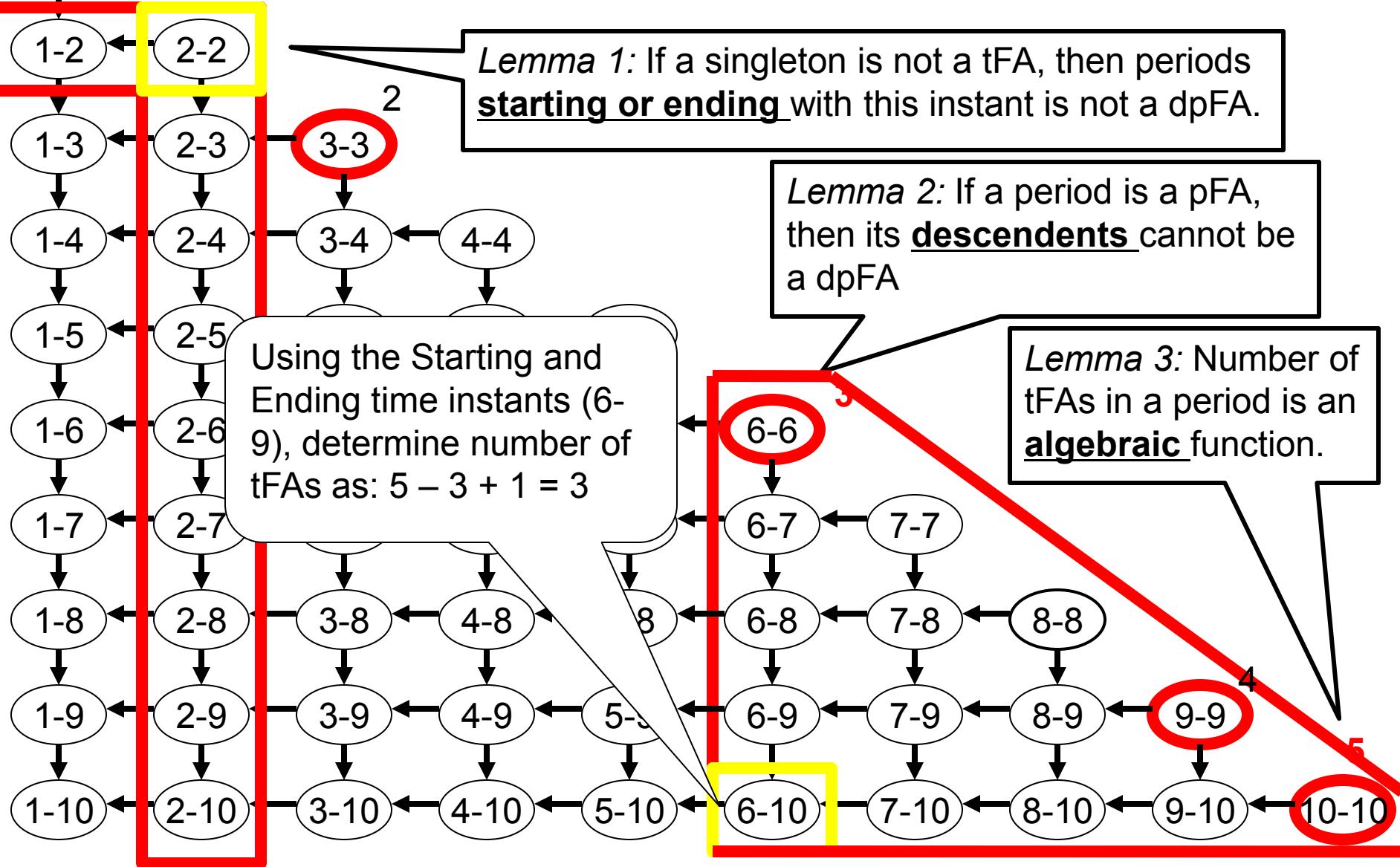
- tFA
- pFA
- Evaluated
- pruned

# Lemma 2: Prune Descents of pfas



# Key Insights to Reduce Computational Cost

1-1 <sup>1</sup>



# *SWEET Approach*

---

- **SWEET Approach**

- Phase 1: Identify the pFAs

- Enumerate and evaluate periods that start and end with a tFA (Lemma 1)

- Phase 2: Identify the dpFAs

- **Design Decisions**

- Smart Counter (Lemma 3)

- Pruning Strategy (Lemma 2)

- **Detail Execution Trace next slide**

- **Computation Cost reduces**

- Naïve:  $O(N)$

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---

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# *SWEET-ER Approach*

## *Key Ideas*

---

- **Disadvantage in both Naïve and SWEET**
  - Exhaustive search of persistent FAs in second phase to find dominant pFAs
- **Expanded Regions**
  - In Phase 1, maintain an index of dominant pFAs as persistent FAs are discovered (Lemma 2)
  - In Phase 2, single scan of ER to identify dominant pFAs

# Analytical Evaluation: Computational Costs

Complexity: (Phase 1 costs + Phase 2 costs)

	Worst Case
Naïve	$n^3 + p^2$
SWEET	$t^3 + p^2$
SWEET [p]	$t^3 + p^2$
SWEET [s]	$t^2 + p^2$
SWEET [s+p]	$t^2 + p^2$
SWEET-ER [s+p]	$t^2 + n$

- **n is the total number of time slots in the dataset**
- **t is the number of tFAs found in the dataset and  $t \leq n$**
- **p is the number of pFAs found in the dataset and  $t \leq p \leq t^2$**

- **Theorem 1 and 3:** SWEET and SWEET-ER are correct, i.e., all discovered patterns satisfy the dpFA definition.
- **Theorem 2 and 4:** SWEET and SWEET-ER are complete, i.e., all dominant pFA patterns are found.

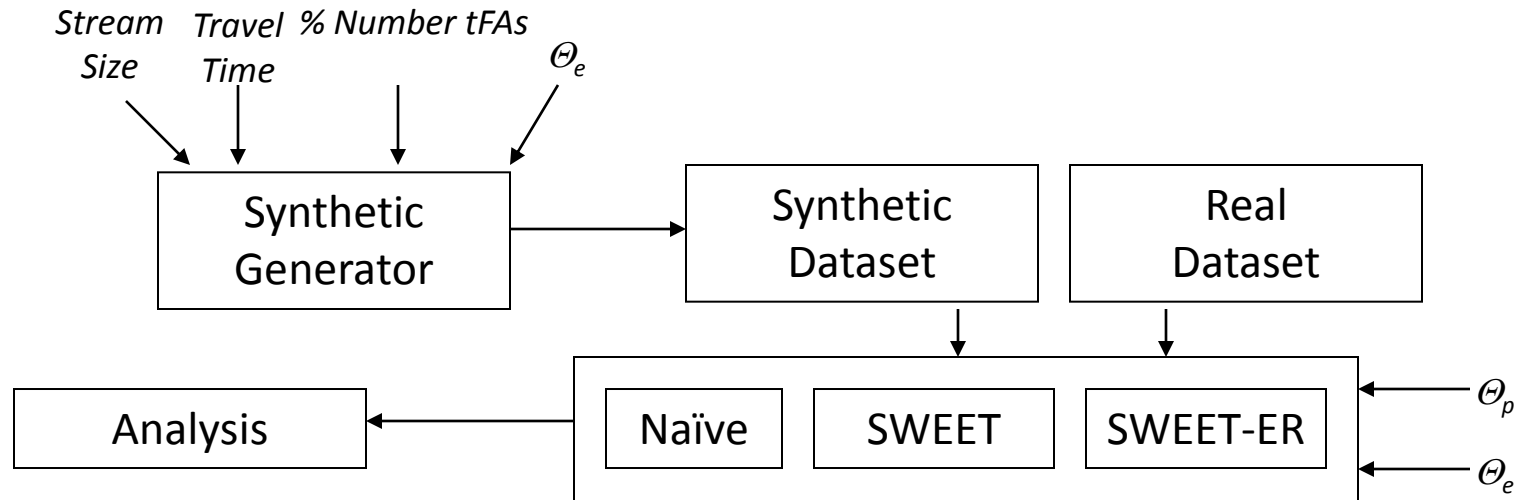


# Outline

---

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# Experimental Evaluation: Setup

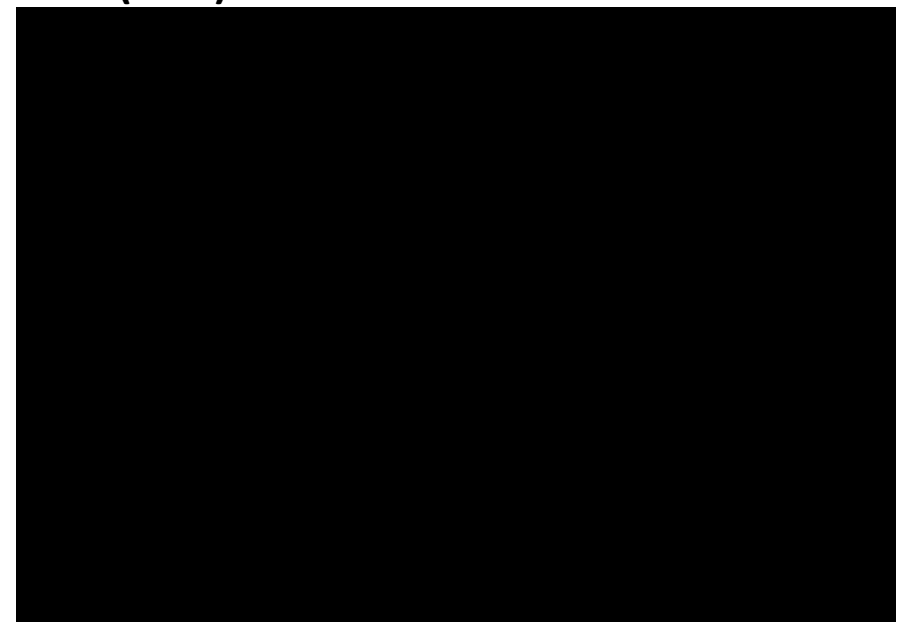
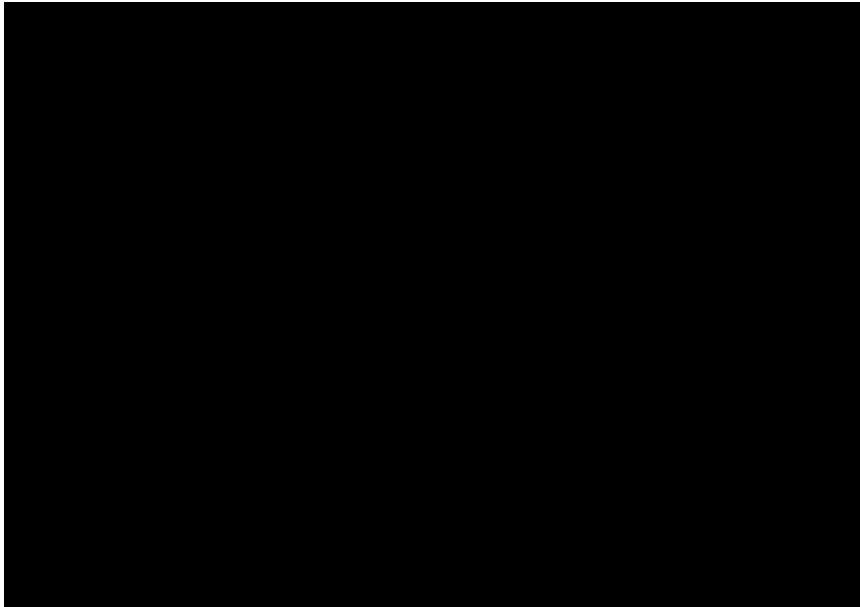


- Experimental Question: What is the effect in the size of the time series?
- Measured in terms of: Execution (CPU) Time
- Methods: Naïve, SWEET, SWEET (s), SWEET (s+p), SWEET-ER (s+p)
- Hardware: P4 2.0 GHz, 1.2 GB RAM

# Synthetic: What is the effect on the size of the time series?

---

## Execution Time (CPU)



### Synthetic Generator Parameters

Travel Time = 10

$\Theta_e = 10$

% # of Anomalies: 30%

### Experimental Parameters

Travel Time = 10

$\Theta_e = 10$

$\Theta_p = 0.80$

At 5K, Naïve takes a little more than **3 hours** to complete, whereas SWEET(s+p) takes a **half a second**

# *Synthetic: What is the effect on the size of the time series?*

---

Execution Time (CPU)



## **Synthetic Generator Parameters**

Travel Time = 10

$\Theta_e = 10$

% # of Anomalies: 10%

## **Experimental Parameters**

Travel Time = 10

$\Theta_e = 10$

$\Theta_p = 0.80$

As expected, SWEET-ER performs far better than SWEET due to the ER index

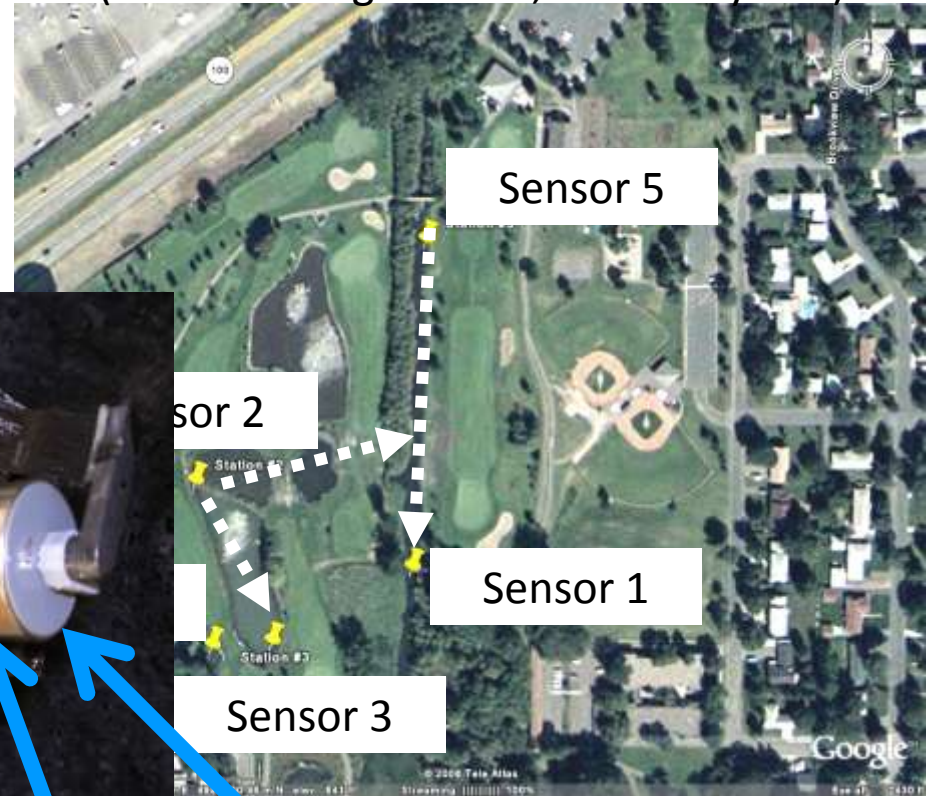
# Real Data Sets

## 1. Shingle Creek

### ① Stations 5 to 1

- Dataset 1: Turbidity: 3K-15K time intervals
- Dataset 2: Dissolved Oxygen: 5K time intervals

(Source: Shingle Creek, MN Study Site)



Sensor 5

Sensor 2

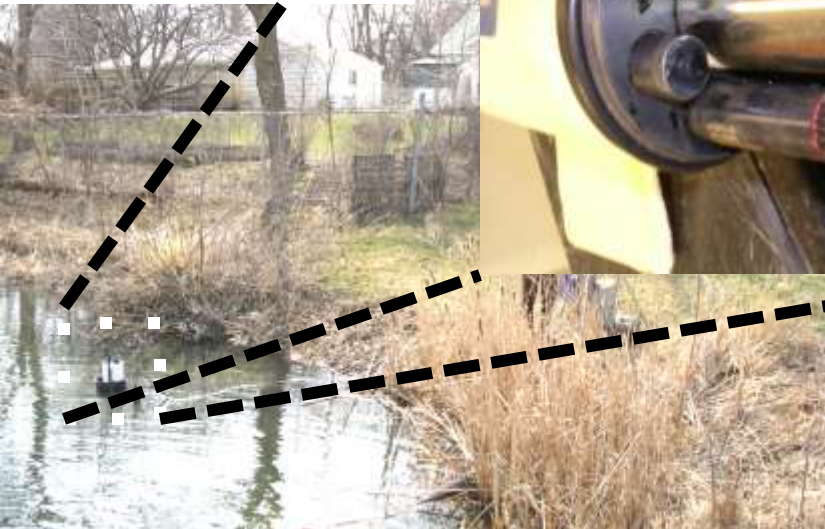
Sensor 1

Sensor 3

Turbidity

Dissolved Oxygen

Sensor Setup



# Wireless Sensor Network



Station #2



Remote Server  
CUAHSI-HIS



Station #4

Base Station:  
Wireless Cellular  
Modem

Data Transfer



Station #1

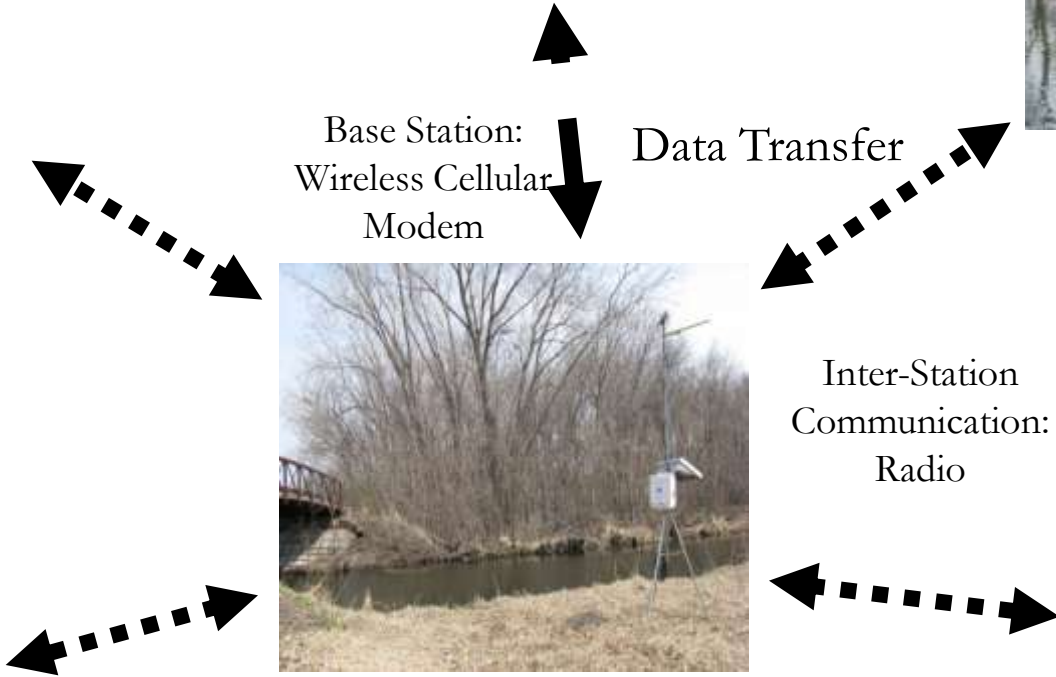
Inter-Station  
Communication:  
Radio



Station #3



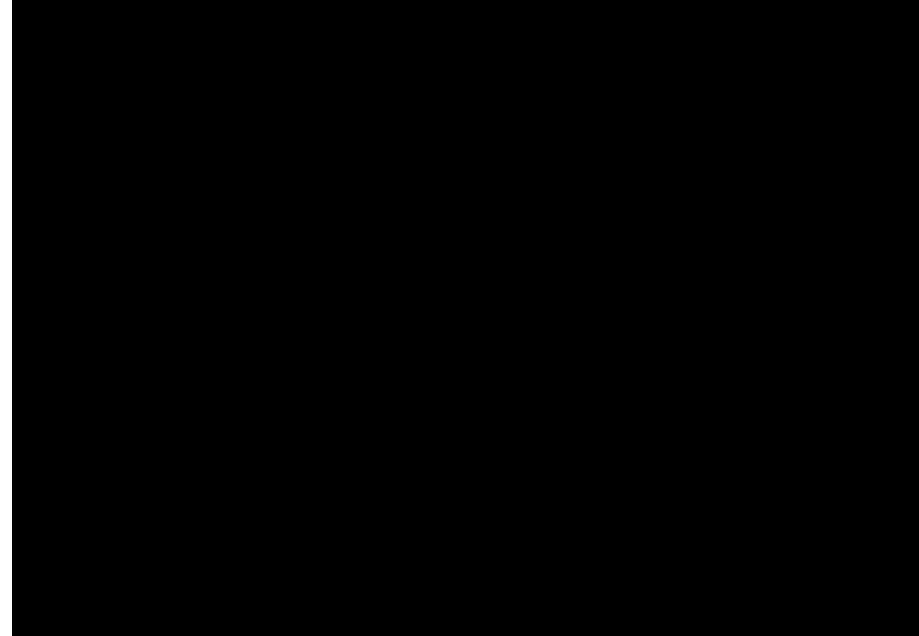
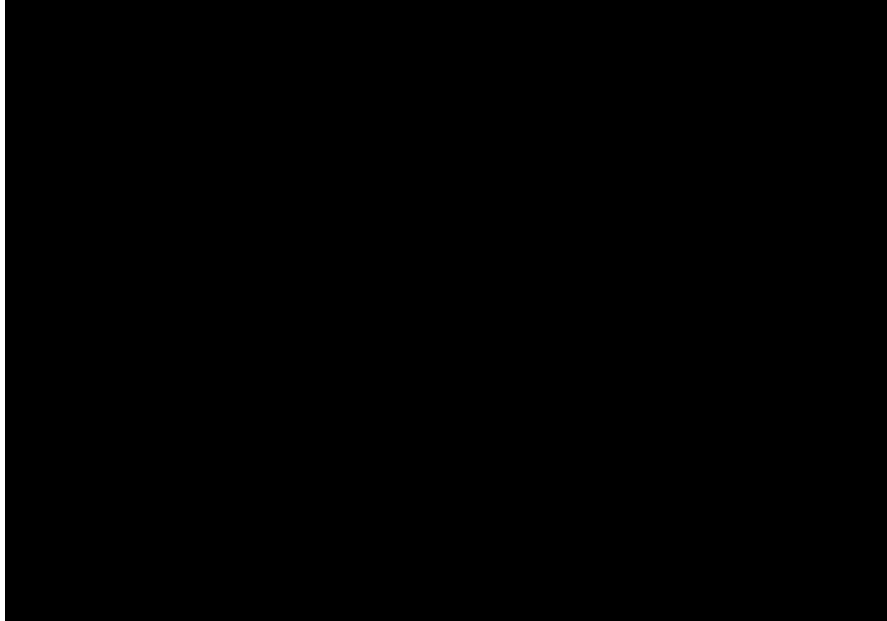
Station #5



## Real Dataset: What is the effect on the size of the time series?

---

### Execution Time (CPU)



#### Experimental Parameters

Travel Time = Variable (From Input)

$$\Theta_e = 10$$

$$\Theta_a = 0.80$$

At 3K, Naïve takes a little more than **1 hour** to complete, whereas SWEET(s+p) takes a **half a second**

# Real Dataset: What is the effect on the size of the time series?

---

Execution Time (CPU)



## Experimental Parameters

Travel Time = Variable (From Input)

$$\Theta_e = 10$$

$$\Theta_a = 0.80$$

Performance gain of SWEET-ER between 12K to 15K due to an increase in number of candidates creating more time needed in SWEET

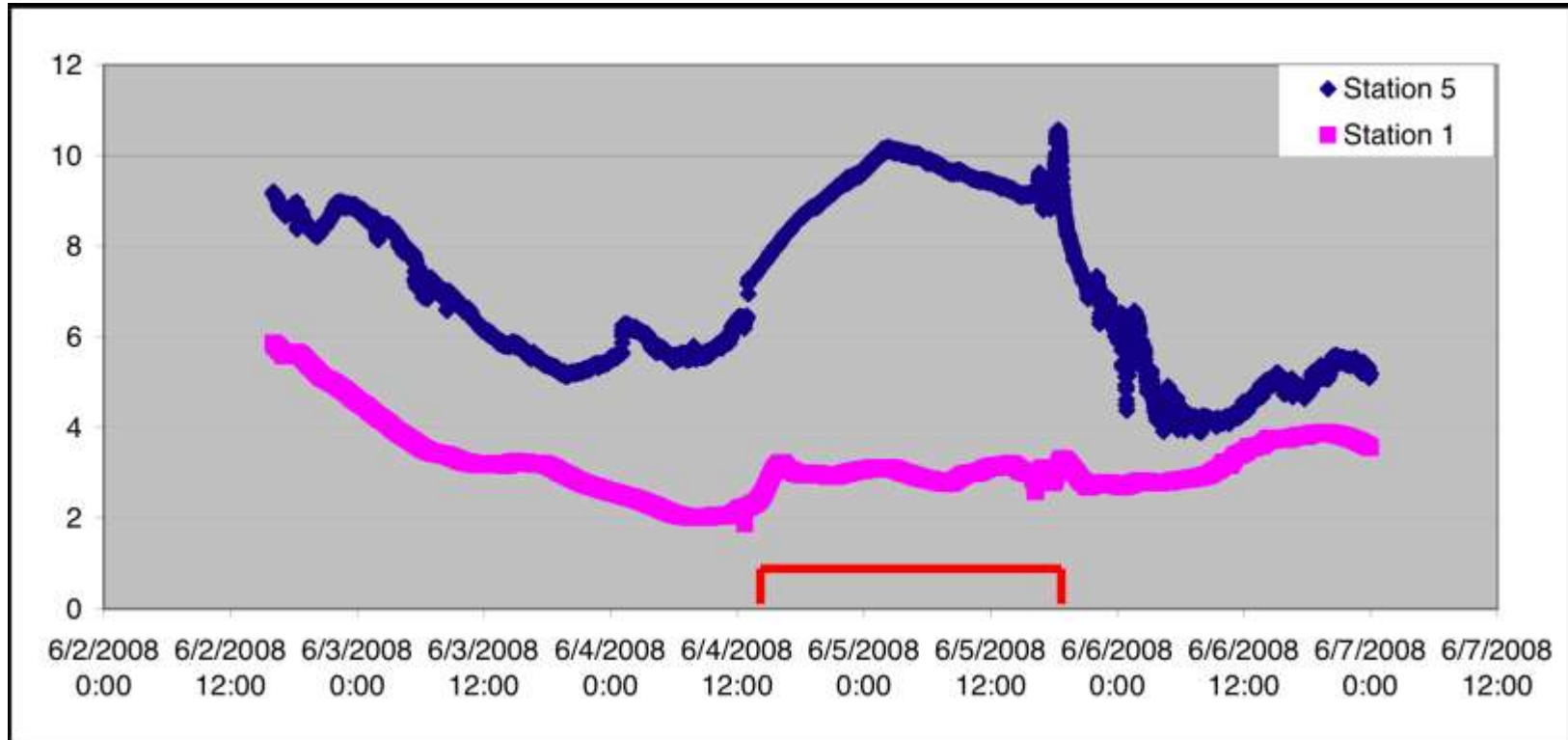


# *Domain-based Validation*

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- 1. What are Flow Anomalies really?**
- 2. Based on the data available, can we determine why a flow anomaly occurred?**

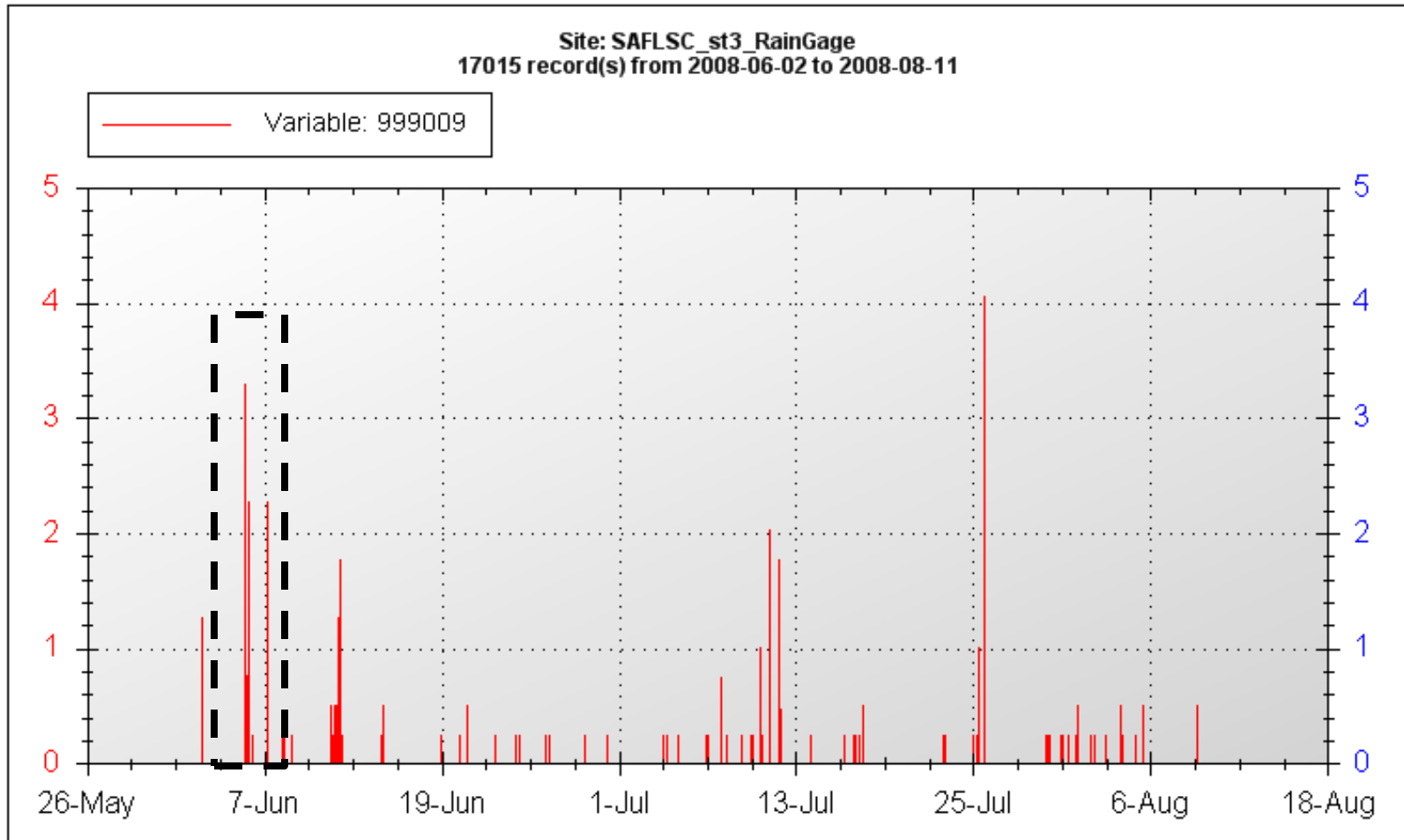
# Domain-based Validation: Dissolved Oxygen



**Longest Flow Anomaly Result** (Error: +/- 5, Persistent: 80%)

Start: 6/4/2008 13:06 End: 6/5/2008 19:34

# Domain-based Validation: Rain Fall



High Rain Fall around June 4-5, 2008 time frame

# Domain-based Validation

---



- 1. It was observed that the retention pond near sensor 4 has very low DO**
- 2. So when a rain event occurs, the water from the pond flushes into the stream between sensors 5 and 1**
- 3. Resulting in a Flow Anomaly for DO**

- **Introduced the FA mining problem and Flow-based Patterns**
  - New concepts and interest measures
  - Proposed Naïve, SWEET and SWEET-ER approaches
- **Analytical Evaluation**
- **Experimental Evaluation**
  - Synthetic and Real Datasets

# Outline

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- Spatial and Spatio-temporal Data Mining
- Environmental Science
- Flow Anomalies
- Gaps, Open Problems

**Domain Modeling**

**Spatio-temporal Data Mining**

# Teleconnected Flow Anomaly

## ■ A Teleconnected Flow Anomaly

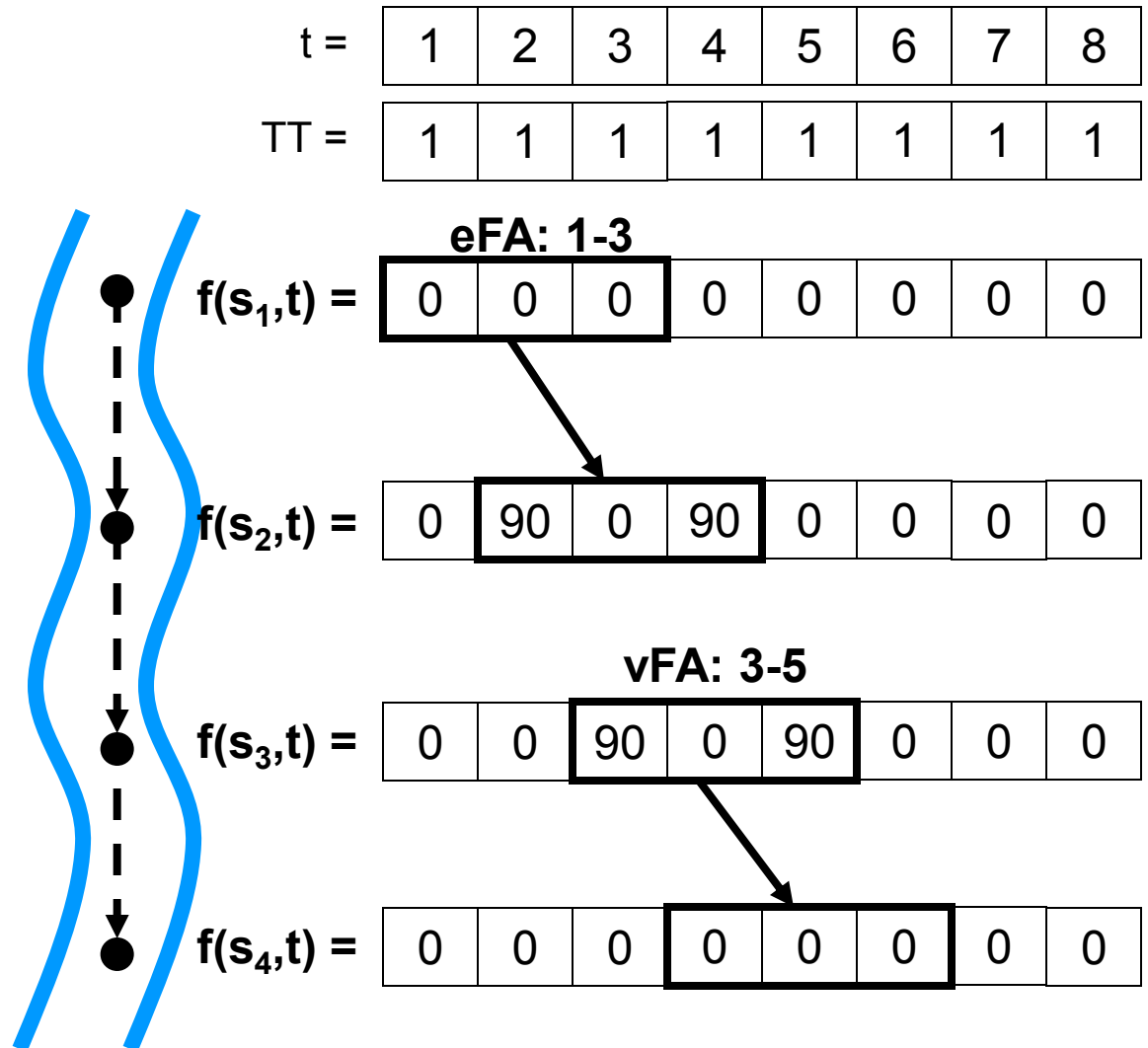
- A pair of FAs based on its velocity field.

## ■ Challenge

- Increase in Combinatorics

## ■ Contributions

- ST Dynamic Neighborhood Model
- RAD Approach



J. M. Kang, S. Shekhar, M. Henjum, P. Novak, W. Arnold, Discovering Teleconnected Flow Anomalies: A Relationship Analysis of spatio-temporal Dynamic (RAD) neighborhoods, *In SSTD*, 2009.

## 1. Understanding of a physical phenomenon

- ① Though, final model may not involve location
  - Cause-effect e.g. Cholera caused by germs
- ② Discovery of model may be aided by spatial patterns
  - Many phenomenon are embedded in space and time
  - Ex. 1854 London – Cholera deaths clustered around a water pump
  - Spatio-temporal process of disease spread => narrow down potential causes
  - Ex. Recent analysis of SARS

## 2. Location helps bring rich contexts

- ① Physical: e.g., rainfall, temperature, and wind
- ② Demographical: e.g., age group, gender, and income type
- ③ Problem-specific, e.g. distance to highway or water



# Future Work cont'd

## Domain-based Computational Challenges

- **Multi-paths and complex networks**
  - Exponential growth in paths



- **Handling mixing for water bodies**
  - 1:M and M:N relationships

- **Uncertainty in Travel Time**
  - All path and All time search for patterns

# Outline

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- Spatial and Spatio-temporal Data Mining
- Environmental Science
- Flow Anomalies
- Gaps, Open Problems

**Domain Modeling**

**Spatio-temporal Data Mining**

# Future Work

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Traditional	Spatial	Spatio-Temporal
Clustering	Hotspot	<b>Spreading Hotspots</b>
Outlier	Spatial Outlier	Flow Anomaly
Association Rules	Co-Locations	Teleconnections
Prediction	Location Prediction	<b>Path Prediction</b>

- **Real-Time Flow Anomalies**

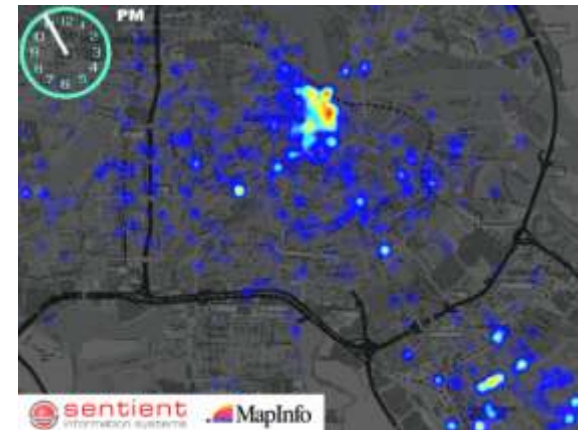
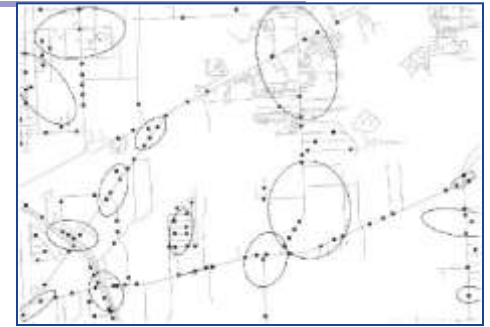
- Discover FA based on a time-constraint

- **Apply Transient, Persistent, Dominant concepts to other spatial pattern families**

- Ex. Hotspot Analysis, Co-locations, etc.

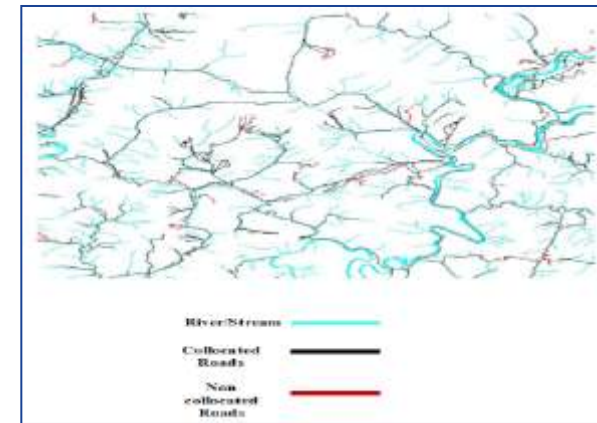
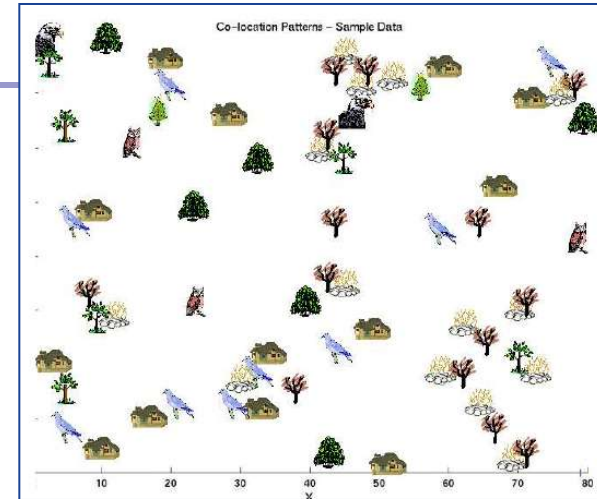
# HotSpots

- What is it?
  - Unusually high spatial concentration of a phenomena
    - Cancer clusters, crime hotspots
- Solved
  - Spatial statistics based ellipsoids
- Almost solved
  - Transportation network based hotspots
- Failed
  - Classical clustering methods, e.g. K-means
- Missing
  - Spatio-temporal
- Next
  - Emerging / Spreading hot-spots



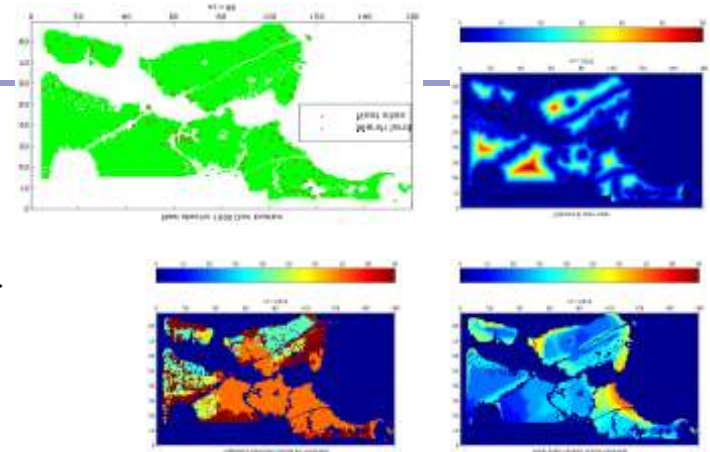
# Colocation, Co-occurrence, Interaction

- What is it?
  - Subset of event types, whose instances occur together
  - Ex. Symbiosis, (bar, misdemeanors), ...
- Solved
  - Colocation of point event-types
- Almost solved
  - Co-location of extended (e.g.linear) objects
  - Object-types that move together
- Failed
  - Neighbor-unaware Transaction based approaches
- Missing
  - Consideration of flow, richer interactions
- Next
  - Spatio-temporal interactions, e.g. item-types that sell well before or after a hurricane
  - Tele-connections



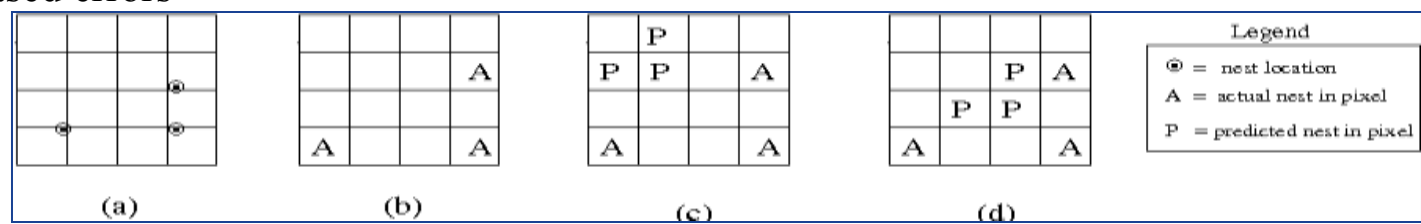
# Space/Time Prediction

- What is it?
  - Models to predict location, time, path, ...
    - Nest sites, minerals, earthquakes, tornadoes, ...
- Solved
  - Interpolation, e.g. Krigging
  - Heterogeneity, e.g. geo. weighted regression
- Almost solved
  - Auto-correlation, e.g. spatial auto-regression
- Failed: Independence assumption
  - Models, e.g. Decision trees, linear regression, ...
  - Measures, e.g. total square error, precision, recall
- Missing
  - Spatio-temporal vector fields (e.g. flows, motion), physics
- Next
  - Scalable algorithms for parameter estimation
  - Distance based errors



$$\mathbf{y} = \rho \mathbf{W} \mathbf{y} + \mathbf{x} \boldsymbol{\beta} + \boldsymbol{\varepsilon}$$

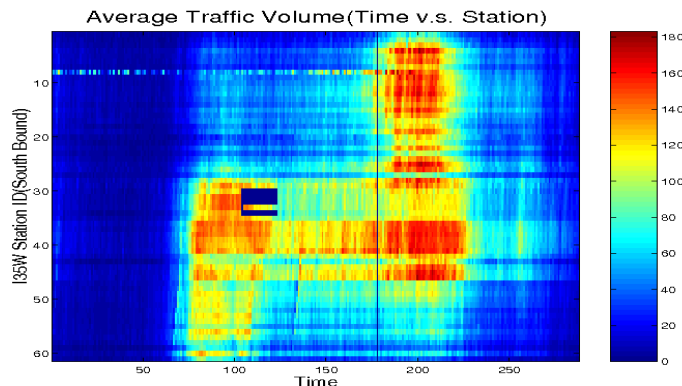
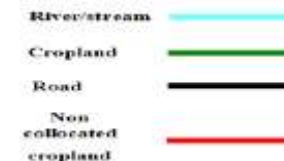
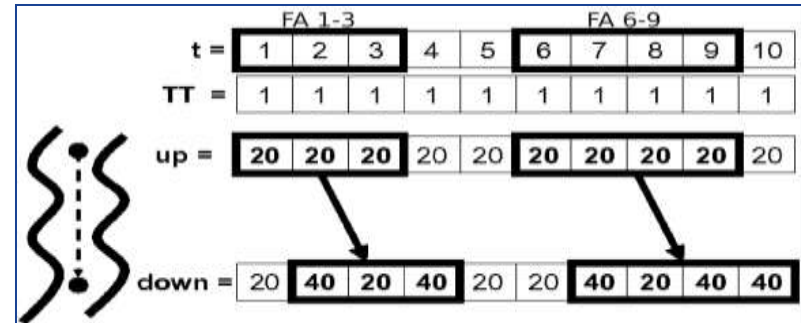
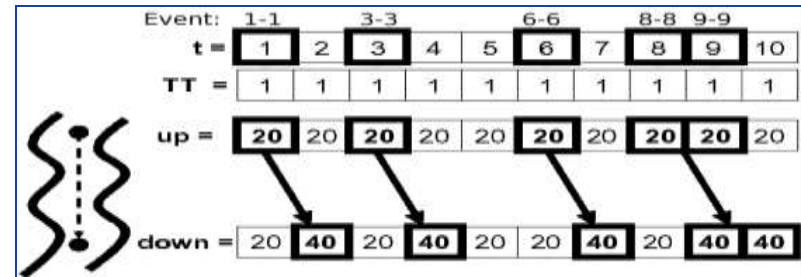
$$\ln(L) = \ln|\mathbf{I} - \rho \mathbf{W}| - \frac{n \ln(2\pi)}{2} - \frac{n \ln(\sigma^2)}{2} - SSE$$





# Spatial/Spatio-temporal Anomalies

- What is it?
  - Location different from their neighbors
    - Discontinuities, flow anomalies
- Solved
  - Transient spatial outliers
- Almost solved
  - Anomalous trajectories
- Failed
- Missing
  - Persistent anomalies
  - Multiple object types, Scale
- Next
  - Multi-criteria Anomalies



# (Geo) Informatics across Disciplines!

